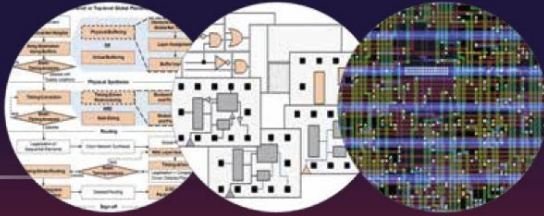


Andrew B. Kahng  
Jens Lienig  
Igor L. Markov  
Jin Hu

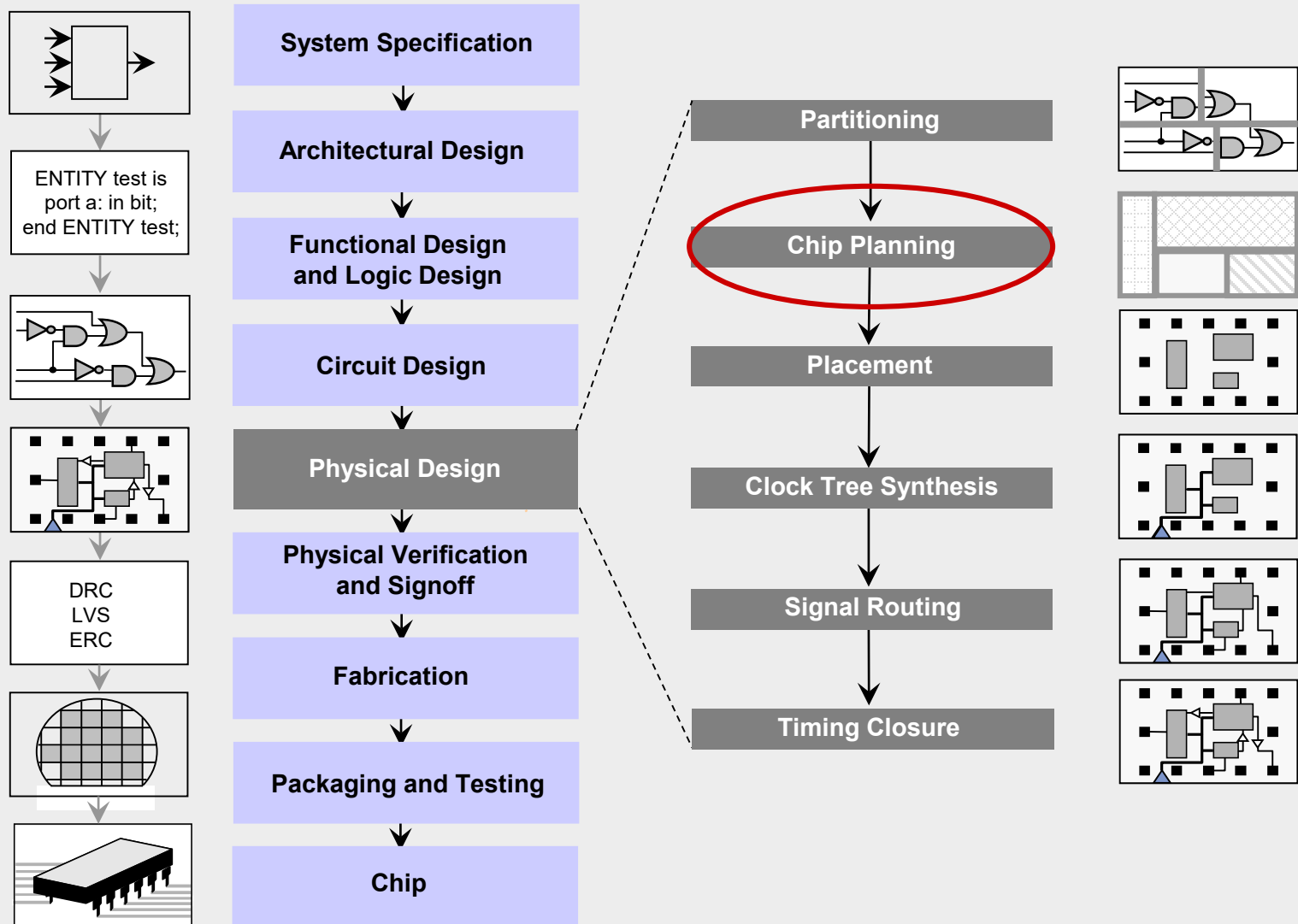


# VLSI Physical Design: From Graph Partitioning to Timing Closure

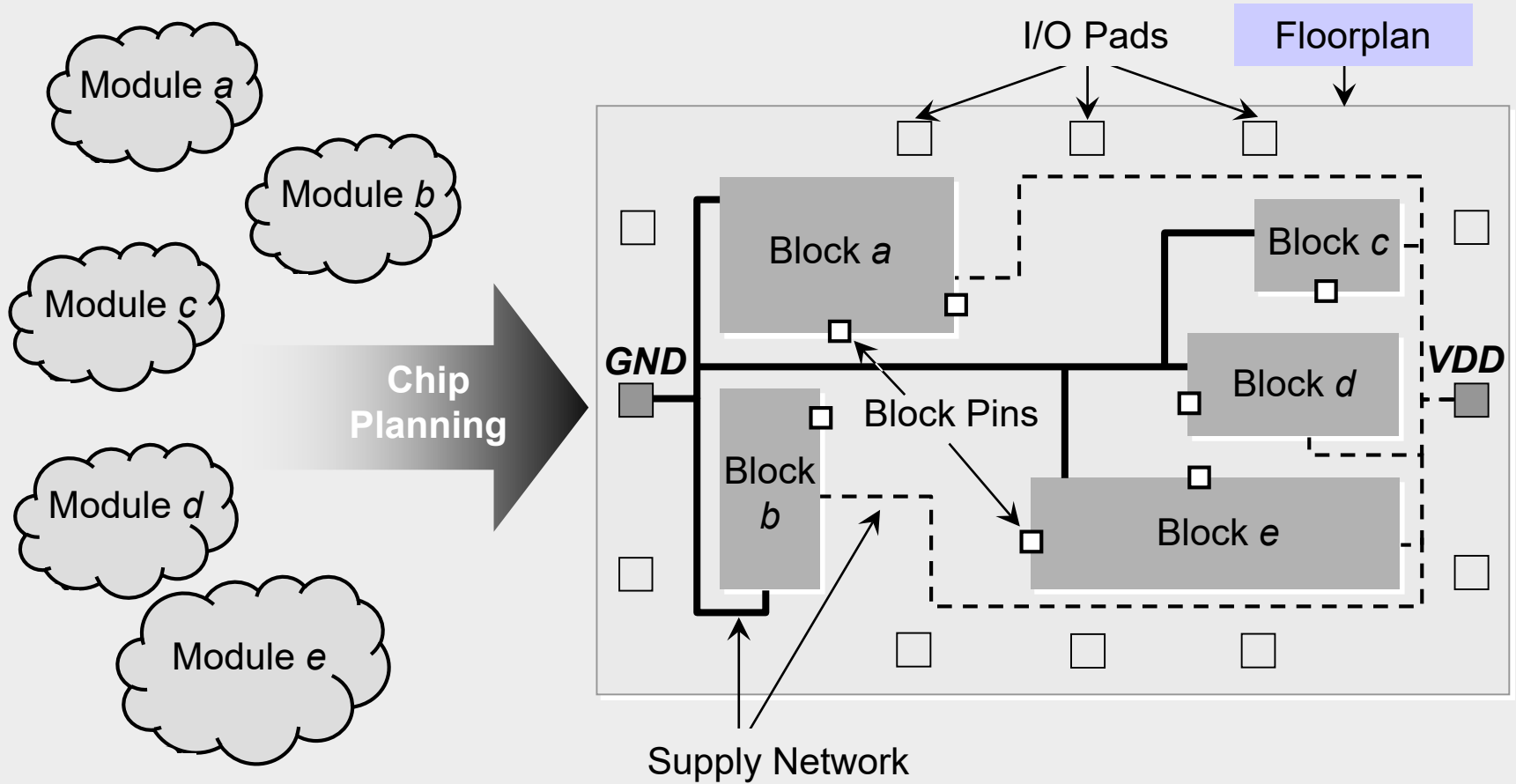
*Second Edition*

## Chapter 3 – Chip Planning

- 3.1 Introduction to Floorplanning
- 3.2 Optimization Goals in Floorplanning
- 3.3 Terminology
- 3.4 Floorplan Representations
  - 3.4.1 Floorplan to a Constraint-Graph Pair
  - 3.4.2 Floorplan to a Sequence Pair
  - 3.4.3 Sequence Pair to a Floorplan
- 3.5 Floorplanning Algorithms
  - 3.5.1 Floorplan Sizing
  - 3.5.2 Cluster Growth
  - 3.5.3 Simulated Annealing
  - 3.5.4 Integrated Floorplanning Algorithms
- 3.6 Pin Assignment
- 3.7 Power and Ground Routing
  - 3.7.1 Design of a Power-Ground Distribution Network
  - 3.7.2 Planar Routing
  - 3.7.3 Mesh Routing



## 3.1 Introduction



## 3.1 Introduction

### Example

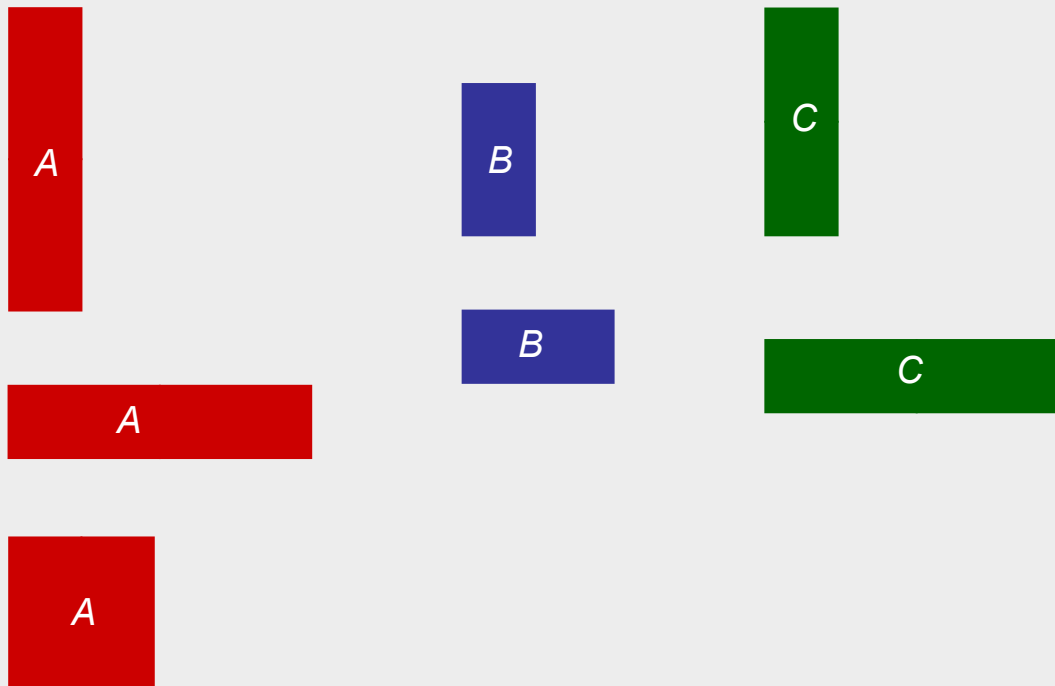
Given: Three blocks with the following potential widths and heights

**Block A:**  $w = 1, h = 4$  or  $w = 4, h = 1$  or  $w = 2, h = 2$

**Block B:**  $w = 1, h = 2$  or  $w = 2, h = 1$

**Block C:**  $w = 1, h = 3$  or  $w = 3, h = 1$

Task: Floorplan with minimum total area enclosed



## 3.1 Introduction

Example

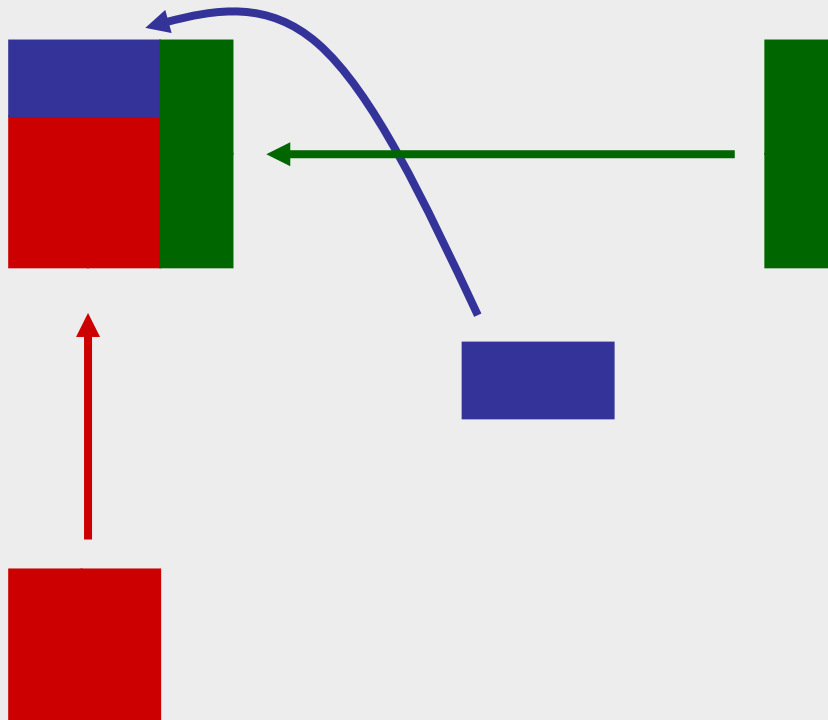
Given: Three blocks with the following potential widths and heights

**Block A:**  $w = 1, h = 4$  or  $w = 4, h = 1$  or  $w = 2, h = 2$

**Block B:**  $w = 1, h = 2$  or  $w = 2, h = 1$

**Block C:**  $w = 1, h = 3$  or  $w = 3, h = 1$

Task: Floorplan with minimum total area enclosed



## 3.1 Introduction

Example

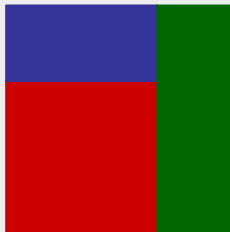
Given: Three blocks with the following potential widths and heights

**Block A:**  $w = 1, h = 4$  or  $w = 4, h = 1$  or  $w = 2, h = 2$

**Block B:**  $w = 1, h = 2$  or  $w = 2, h = 1$

**Block C:**  $w = 1, h = 3$  or  $w = 3, h = 1$

Task: Floorplan with minimum total area enclosed



Solution:

Aspect ratios

**Block A** with  $w = 2, h = 2$ ; **Block B** with  $w = 2, h = 1$ ; **Block C** with  $w = 1, h = 3$

This floorplan has a global bounding box with minimum possible area (9 square units).

## 3.2 Optimization Goals in Floorplanning

- Area and shape of the global bounding box
  - Global bounding box of a floorplan is the minimum axis-aligned rectangle that contains all floorplan blocks.
  - Area of the global bounding box represents the area of the top-level floorplan
  - Minimizing the area involves finding  $(x,y)$  locations, as well as shapes, of the individual blocks.
- Total wirelength
  - Long connections between blocks may increase signal propagation delays in the design.
- Combination of area  $area(F)$  and total wirelength  $L(F)$  of floorplan  $F$ 
  - Minimize  $\alpha \cdot area(F) + (1 - \alpha) \cdot L(F)$   
where the parameter  $0 \leq \alpha \leq 1$  gives the relative importance between  $area(F)$  and  $L(F)$
- Signal delays
  - Static timing analysis is used to identify the interconnects that lie on critical paths.

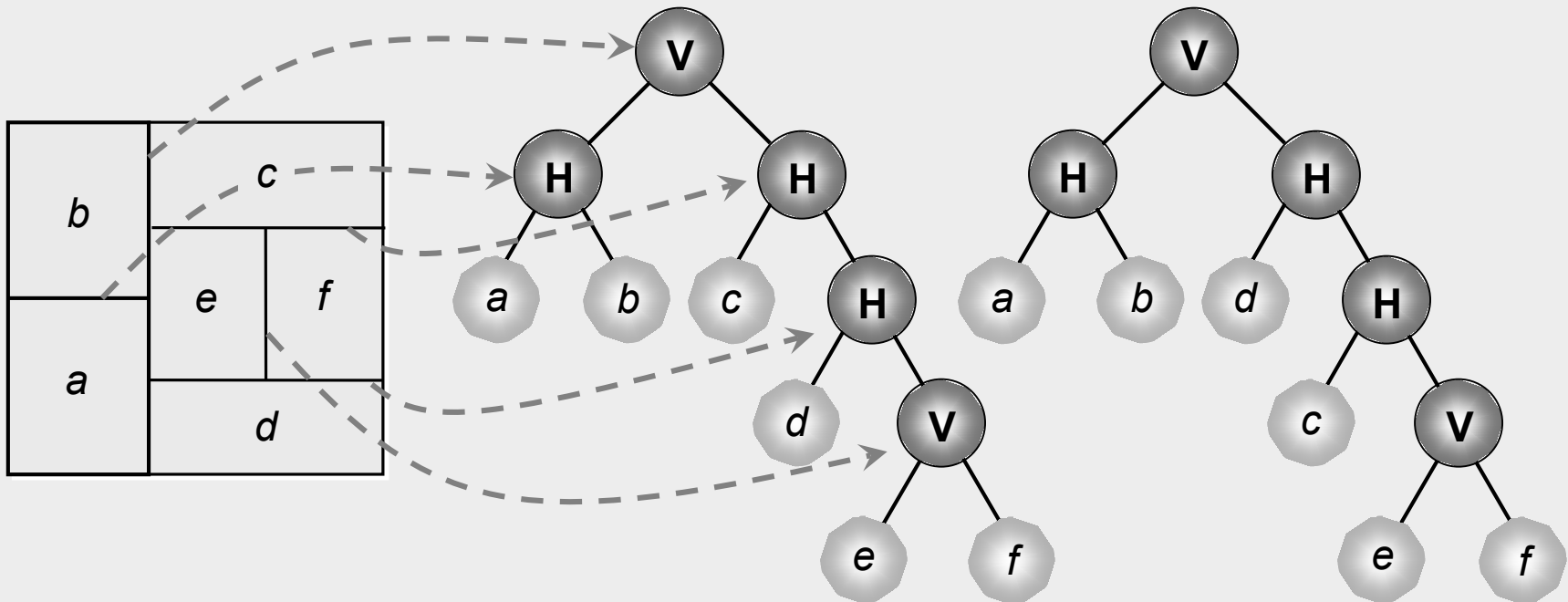


### 3.3 Terminology

- A **rectangular dissection** is a division of the chip area into a set of *blocks* or non-overlapping rectangles.
- A **slicing floorplan** is a rectangular dissection
  - Obtained by repeatedly dividing each rectangle, starting with the entire chip area, into two smaller rectangles
  - Horizontal or vertical cut line.
- A **slicing tree** or **slicing floorplan tree** is a binary tree with  $k$  leaves and  $k - 1$  internal nodes
  - Each leaf represents a block
  - Each internal node represents a horizontal or vertical cut line.

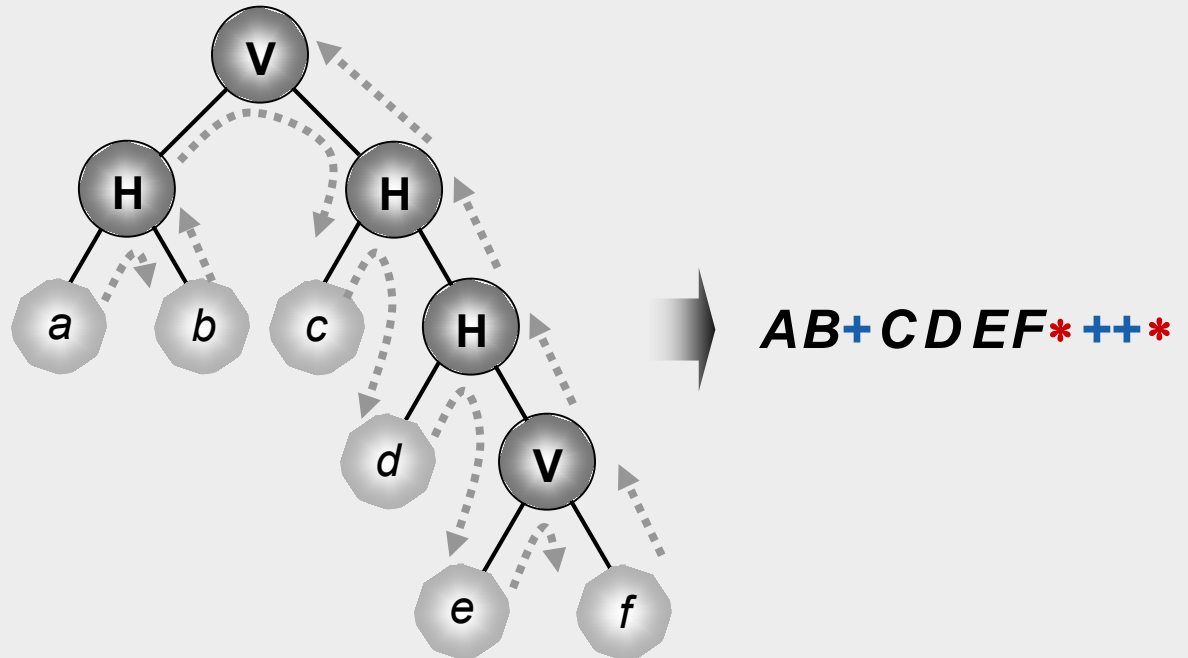
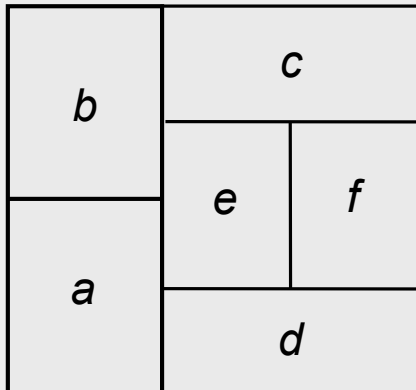
### 3.3 Terminology

Slicing floorplan and two possible corresponding slicing trees



### 3.3 Terminology

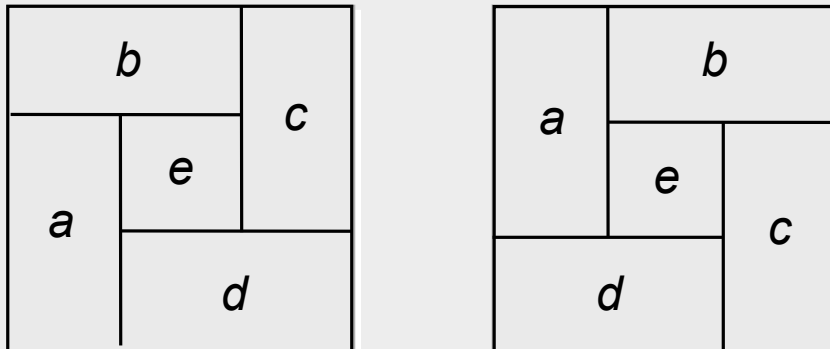
Polish expression



- Bottom up:  $V \rightarrow *$  and  $H \rightarrow +$
- Length  $2n-1$  ( $n$  = Number of leaves of the slicing tree)

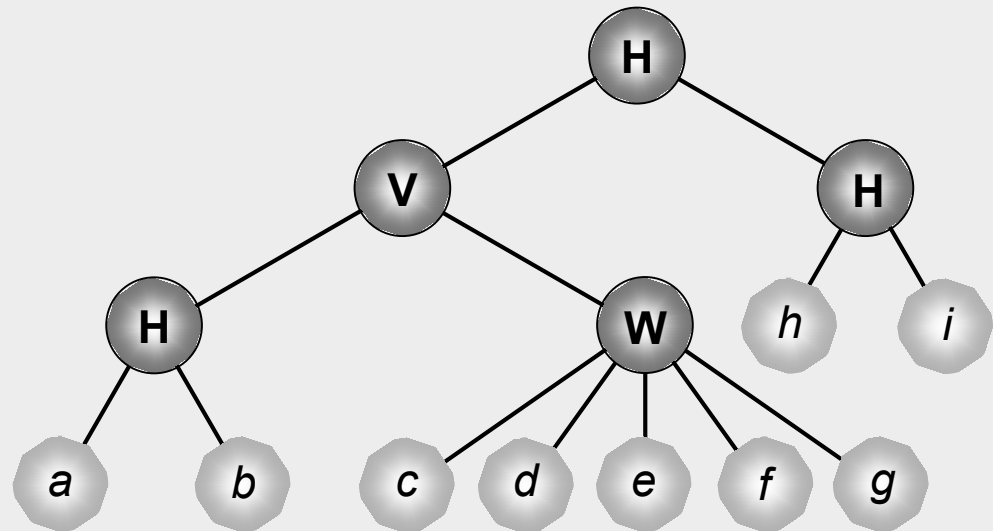
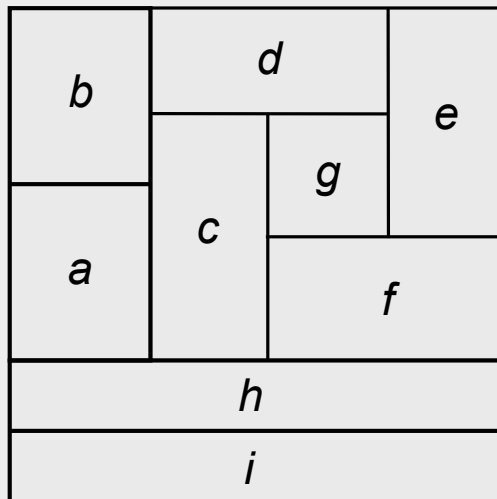
### 3.3 Terminology

#### Non-slicing floorplans (wheels)



### 3.3 Terminology

Floorplan tree: Tree that represents a hierarchical floorplan



- H** Horizontal division  
(objects to the top and bottom)
- V** Vertical division  
(objects to the left and right)

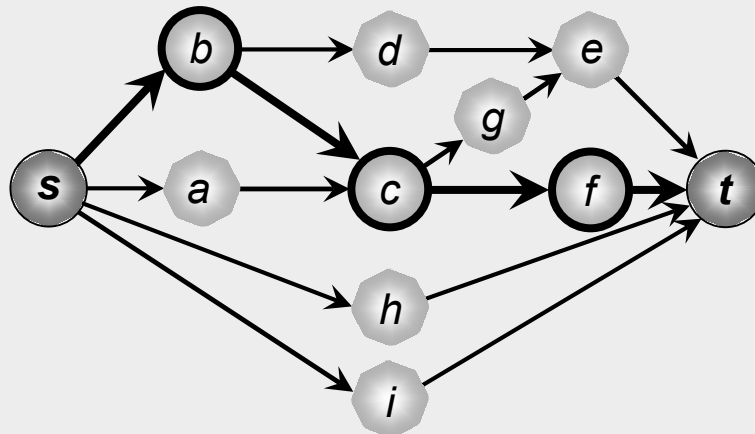
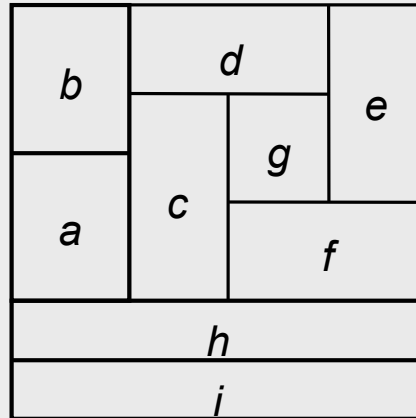
- W** Wheel (4 objects cycled  
around a center object)

### 3.3 Terminology

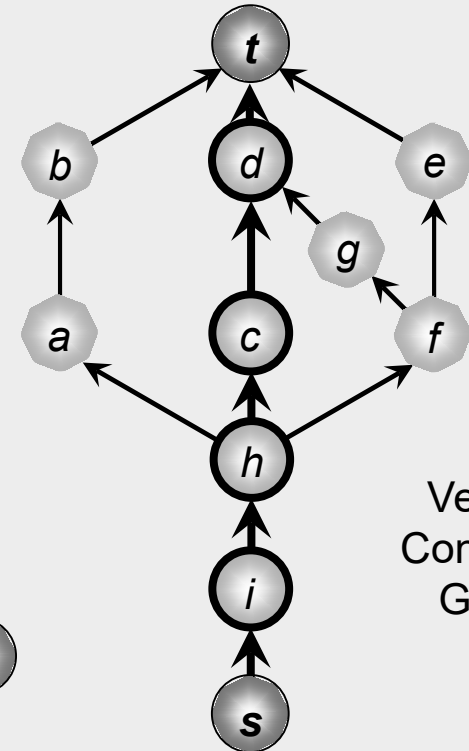
- In a **vertical constraint graph (VCG)**, node weights represent the heights of the corresponding blocks.
  - Two nodes  $v_i$  and  $v_j$ , with corresponding blocks  $m_i$  and  $m_j$ , are connected with a directed edge from  $v_i$  to  $v_j$  if  $m_i$  is below  $m_j$ .
- In a **horizontal constraint graph (HCG)**, node weights represent the widths of the corresponding blocks.
  - Two nodes  $v_i$  and  $v_j$ , with corresponding blocks  $m_i$  and  $m_j$ , are connected with a directed edge from  $v_i$  to  $v_j$  if  $m_i$  is to the left of  $m_j$ .
- The longest path(s) in the VCG / HCG correspond(s) to the minimum vertical / horizontal floorplan span required to pack the blocks (floorplan height / width).
- A **constraint-graph pair** is a floorplan representation that consists of two directed graphs – *vertical constraint graph* and *horizontal constraint graph* – which capture the relations between block positions.

### 3.3 Terminology

#### Constraint graphs



Horizontal Constraint Graph

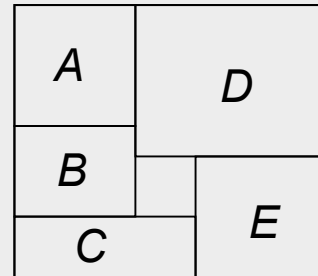


Vertical  
Constraint  
Graph

### 3.3 Terminology

#### Sequence pair

- Two permutations represent geometric relations between every pair of blocks
- Example: ( $ABDCE$ ,  $CBAED$ )



- Horizontal and vertical relations between blocks  $A$  and  $B$ :

$(\dots A \dots B \dots, \dots A \dots B \dots) \rightarrow A$  is left of  $B$

$(\dots A \dots B \dots, \dots B \dots A \dots) \rightarrow A$  is above  $B$

$(\dots B \dots A \dots, \dots A \dots B \dots) \rightarrow A$  is below  $B$

$(\dots B \dots A \dots, \dots B \dots A \dots) \rightarrow A$  is right of  $B$




## 3.4 Floorplan Representations

3.1 Introduction to Floorplanning

3.2 Optimization Goals in Floorplanning

3.3 Terminology

 3.4 Floorplan Representations

3.4.1 Floorplan to a Constraint-Graph Pair

3.4.2 Floorplan to a Sequence Pair

3.4.3 Sequence Pair to a Floorplan

3.5 Floorplanning Algorithms

3.5.1 Floorplan Sizing

3.5.2 Cluster Growth

3.5.3 Simulated Annealing

3.5.4 Integrated Floorplanning Algorithms

3.6 Pin Assignment

3.7 Power and Ground Routing

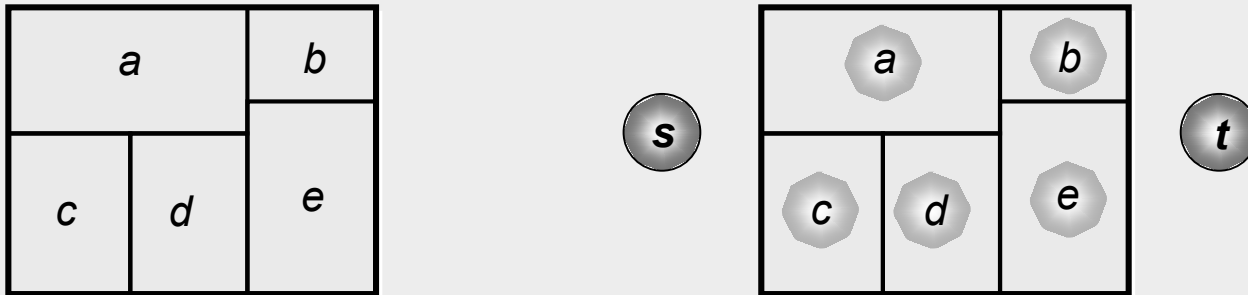
3.7.1 Design of a Power-Ground Distribution Network

3.7.2 Planar Routing

3.7.3 Mesh Routing

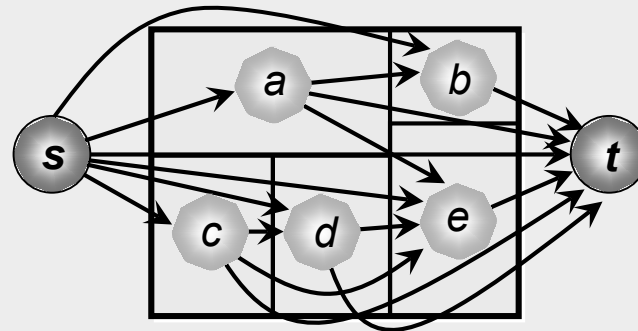
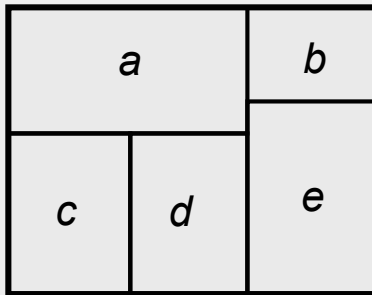
### 3.4.1 Floorplan to a Constraint-Graph Pair

- Create nodes for every block
- In addition, create a source node and a sink one



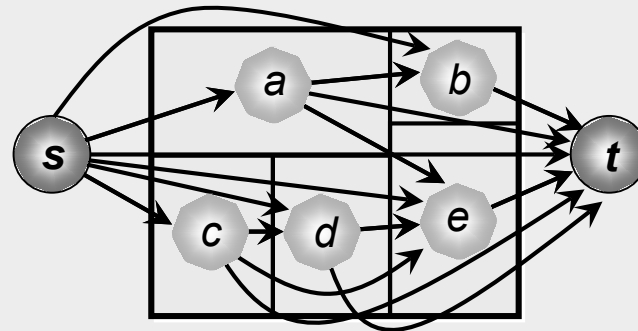
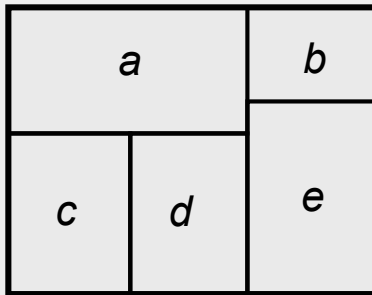
### 3.4.1 Floorplan to a Constraint-Graph Pair

- Create nodes for every block.
- In addition, create a source node and a sink one.
- Add a directed edge  $(A,B)$  if Block  $A$  is below/left of Block  $B$ . (HCG)



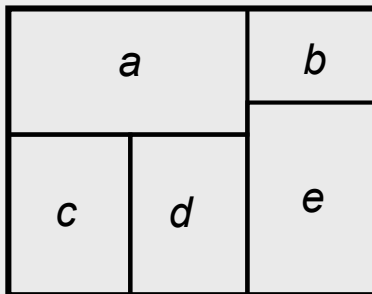
### 3.4.1 Floorplan to a Constraint-Graph Pair

- Create nodes for every block.
- In addition, create a source node and a sink one.
- Add a directed edge  $(A,B)$  if Block  $A$  is below/left of Block  $B$ . (HCG)
- Remove the redundant edges that can be derived from other edges by transitivity.



### 3.4.2 Floorplan to a Sequence Pair

- Given two blocks  $A$  and  $B$  with
  - Locations:  $A = (x_A, y_A)$  and  $B = (x_B, y_B)$
  - Dimensions:  $A = (w_A, h_A)$  and  $B = (w_B, h_B)$
- If  $x_A + w_A \leq x_B$  and  $!(y_A + h_A \leq y_B \text{ or } y_B + h_B \leq y_A)$ , then  $A$  is **left of**  $B$
- If  $y_A + h_A \leq y_B$  and  $!(x_A + w_A \leq x_B \text{ or } x_B + w_B \leq x_A)$ , then  $A$  is **below**  $B$



$$S_+ :< acdbe >$$

$$S_- :< cdaeb >$$

### 3.4.3 Sequence Pair to a Floorplan

- Start with the bottom left corner
- Define a *weighted sequence* as a sequence of blocks based on width
  - Each block  $B$  has its own width  $w(B)$
- Old (traditional) algorithm: find the longest path through edges ( $O(n^2)$ )
- Newer approach: find the *longest common subsequence (LCS)*
  - Given two weighted sequences  $S_1$  and  $S_2$ , the  $LCS(S_1, S_2)$  is the longest sequence found in both  $S_1$  and  $S_2$
  - The length of  $LCS(S_1, S_2)$  is the sum of weights
- For block placement:
  - $LCS(S_+, S_-)$  returns the x-coordinates of all blocks
  - $LCS(S_+^R, S_-)$  returns the y-coordinates of all blocks ( $S_+^R$  is the reverse of  $S_+$ )
  - The length of  $LCS(S_+, S_-)$  and  $LCS(S_+^R, S_-)$  is the width and height, respectively

### 3.4.3 Sequence Pair to a Floorplan

Algorithm: Longest Common Subsequence (LCS)

Input: sequences  $S_1$  and  $S_2$ , weights of  $n$  blocks *weights*

Output: positions of each block *positions*, total span  $L$

```
1.  for ( $i = 1$  to  $n$ )                                // initialization
2.     $block\_order[S_2[i]] = i$ 
3.     $lengths[i] = 0$ 
4.  for ( $i = 1$  to  $n$ )
5.     $block = S_1[i]$                                     // current block
6.     $index = block\_order[block]$ 
7.     $positions[block] = lengths[index]$                 // compute block position
8.     $t\_span = positions[block] + weights[block]$         // finds length of sequence
                                                                // from beginning to block
9.    for ( $j = index$  to  $n$ )                            // update total length
10.     if ( $t\_span > lengths[j]$ )  $lengths[j] = t\_span$ 
11.     else break
12.  $L = lengths[n]$                                     // total length is stored here
```

### 3.4.3 Sequence Pair to a Floorplan

Example:  $S_1 = \langle acdbe \rangle$ ,  $S_2 = \langle cdaeb \rangle$ ,  
 $widths[a\ b\ c\ d\ e] = [8\ 4\ 4\ 4\ 4]$ ,  $heights[a\ b\ c\ d\ e] = [4\ 2\ 5\ 5\ 6]$

Find x-coordinates – go by  $S_1$ 's order:

Initial:  $block\_order[a\ b\ c\ d\ e] = [3\ 5\ 1\ 2\ 4]$ ,  $lengths = [0\ 0\ 0\ 0\ 0]$

Iteration 1 – block = **a**, index = **3**:

$positions[a] = lengths[3] = 0$ ,  $t\_span = 8$ ,  $lengths = [0\ 0\ 8\ 8\ 8]$

Iteration 2 – block = **c**, index = **1**:

$positions[c] = lengths[1] = 0$ ,  $t\_span = 4$ ,  $lengths = [4\ 4\ 8\ 8\ 8]$

Iteration 3 – block = **d**, index = **2**:

$positions[d] = lengths[2] = 4$ ,  $t\_span = 8$ ,  $lengths = [4\ 8\ 8\ 8\ 8]$

Iteration 4 – block = **b**, index = **5**:

$positions[b] = lengths[5] = 8$ ,  $t\_span = 12$ ,  $lengths = [4\ 8\ 8\ 8\ 12]$

Iteration 5 – block = **e**, index = **4**:

$positions[e] = lengths[4] = 8$ ,  $t\_span = 12$ ,  $lengths = [4\ 8\ 8\ 12\ 12]$

$positions[a\ b\ c\ d\ e] = [0\ 8\ 0\ 4\ 8]$ ,  $total\_width = lengths[n = 5] = 12$



### 3.4.3 Sequence Pair to a Floorplan

Example:  $S_1 = \langle acdbe \rangle$ ,  $S_2 = \langle cdaeb \rangle$ ,  
 $widths[a\ b\ c\ d\ e] = [8\ 4\ 4\ 4\ 4]$ ,  $heights[a\ b\ c\ d\ e] = [4\ 2\ 5\ 5\ 6]$

Find y-coordinates – go by  $S_1^R$ 's order:

Initial:  $block\_order[a\ b\ c\ d\ e] = [3\ 5\ 1\ 2\ 4]$ ,  $lengths = [0\ 0\ 0\ 0\ 0]$

Iteration 1 – block = **e**, index = **4**:

$positions[e] = lengths[4] = 0$ ,  $t\_span = 6$ ,  $lengths = [0\ 0\ 0\ \mathbf{6}\ \mathbf{6}]$

Iteration 2 – block = **b**, index = **5**:

$positions[b] = lengths[5] = 6$ ,  $t\_span = 9$ ,  $lengths = [0\ 0\ 0\ 6\ \mathbf{9}]$

Iteration 3 – block = **d**, index = **2**:

$positions[d] = lengths[2] = 0$ ,  $t\_span = 5$ ,  $lengths = [0\ \mathbf{5}\ \mathbf{5}\ 6\ 9]$

Iteration 4 – block = **c**, index = **1**:


$positions[c] = lengths[1] = 0$ ,  $t\_span = 5$ ,  $lengths = [\mathbf{5}\ \mathbf{5}\ \mathbf{5}\ 6\ 9]$

Iteration 5 – block = **a**, index = **3**:

$positions[a] = lengths[3] = 5$ ,  $t\_span = 9$ ,  $lengths = [5\ 5\ \mathbf{9}\ \mathbf{9}\ \mathbf{9}]$

$positions[a\ b\ c\ d\ e] = [5\ 6\ 0\ 0\ 0]$ ,  $total\_height = lengths[n = 5] = 9$

## 3.5 Floorplanning Algorithms

- 3.1 Introduction to Floorplanning
- 3.2 Optimization Goals in Floorplanning
- 3.3 Terminology
- 3.4 Floorplan Representations
  - 3.4.1 Floorplan to a Constraint-Graph Pair
  - 3.4.2 Floorplan to a Sequence Pair
  - 3.4.3 Sequence Pair to a Floorplan
-  3.5 Floorplanning Algorithms
  - 3.5.1 Floorplan Sizing
  - 3.5.2 Cluster Growth
  - 3.5.3 Simulated Annealing
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  - 3.7.3 Mesh Routing

## 3.5 Floorplanning Algorithms

### Common Goals

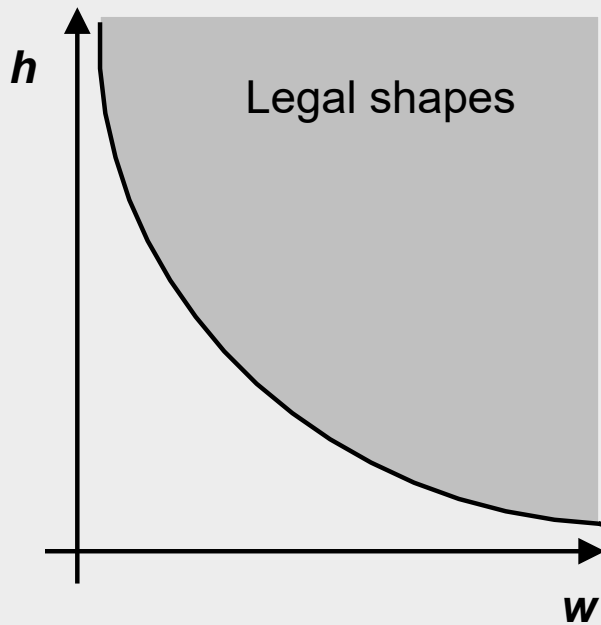
- To minimize the total length of interconnect, subject to an upper bound on the floorplan area

or

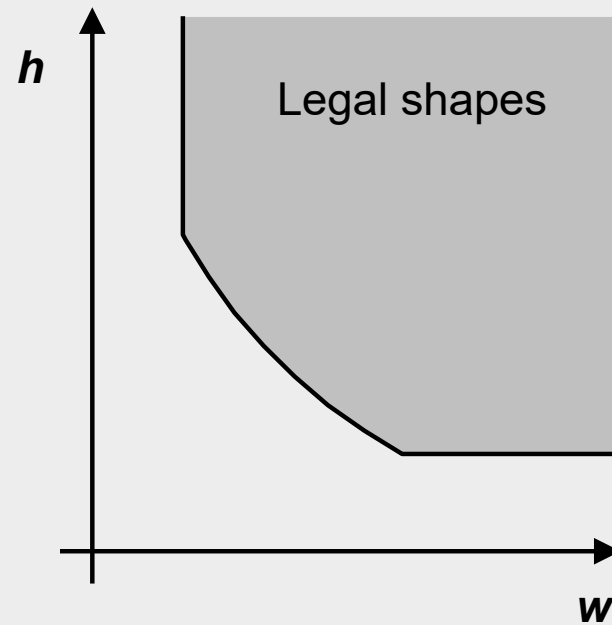
- To simultaneously optimize both wire length and area

## 3.5.1 Floorplan Sizing

### Shape functions



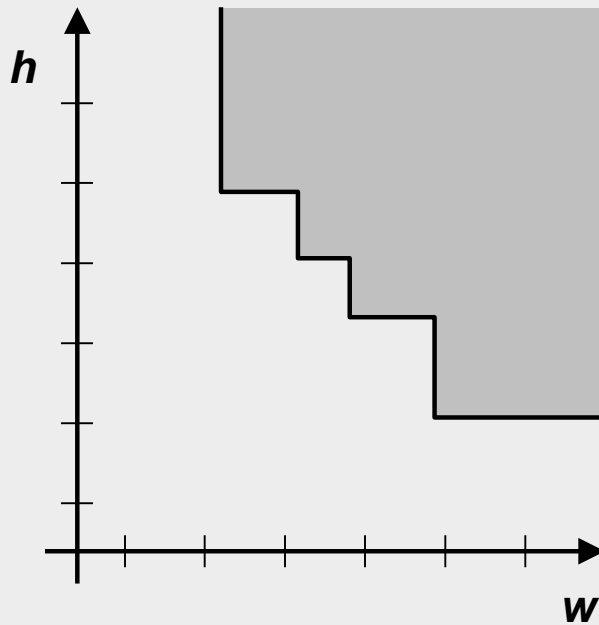
$$h * w \geq A$$



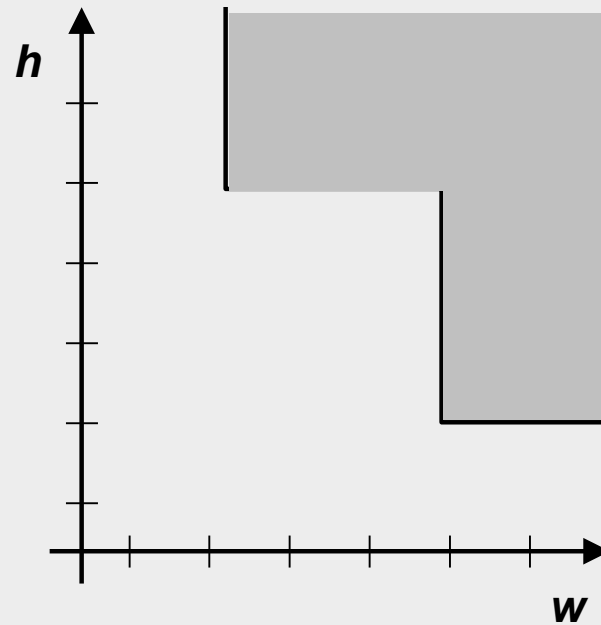
Block with minimum width and height restrictions

## 3.5.1 Floorplan Sizing

### Shape functions



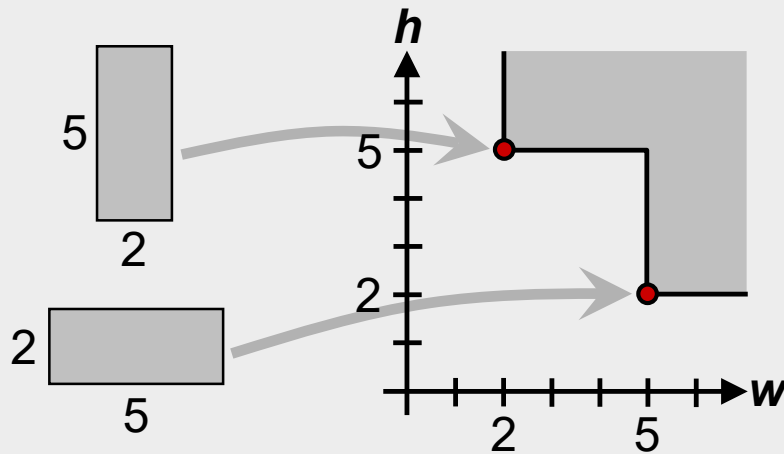
Discrete  $(h, w)$  values



Hard library block

## 3.5.1 Floorplan Sizing

### Corner points



## 3.5.1 Floorplan Sizing

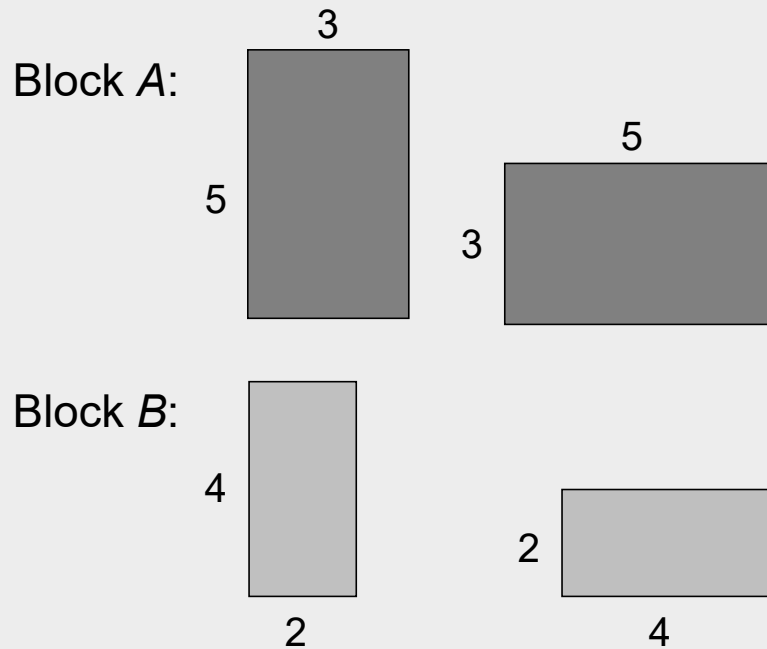
### Algorithm

This algorithm finds the **minimum floorplan area** for a given slicing floorplan in polynomial time. For non-slicing floorplans, the problem is NP-hard.

- Construct the shape functions of all individual blocks
- Bottom up: Determine the shape function of the top-level floorplan from the shape functions of the individual blocks
- Top down: From the corner point that corresponds to the minimum top-level floorplan area, trace back to each block's shape function to find that block's dimensions and location.

### 3.5.1 Floorplan Sizing – Example

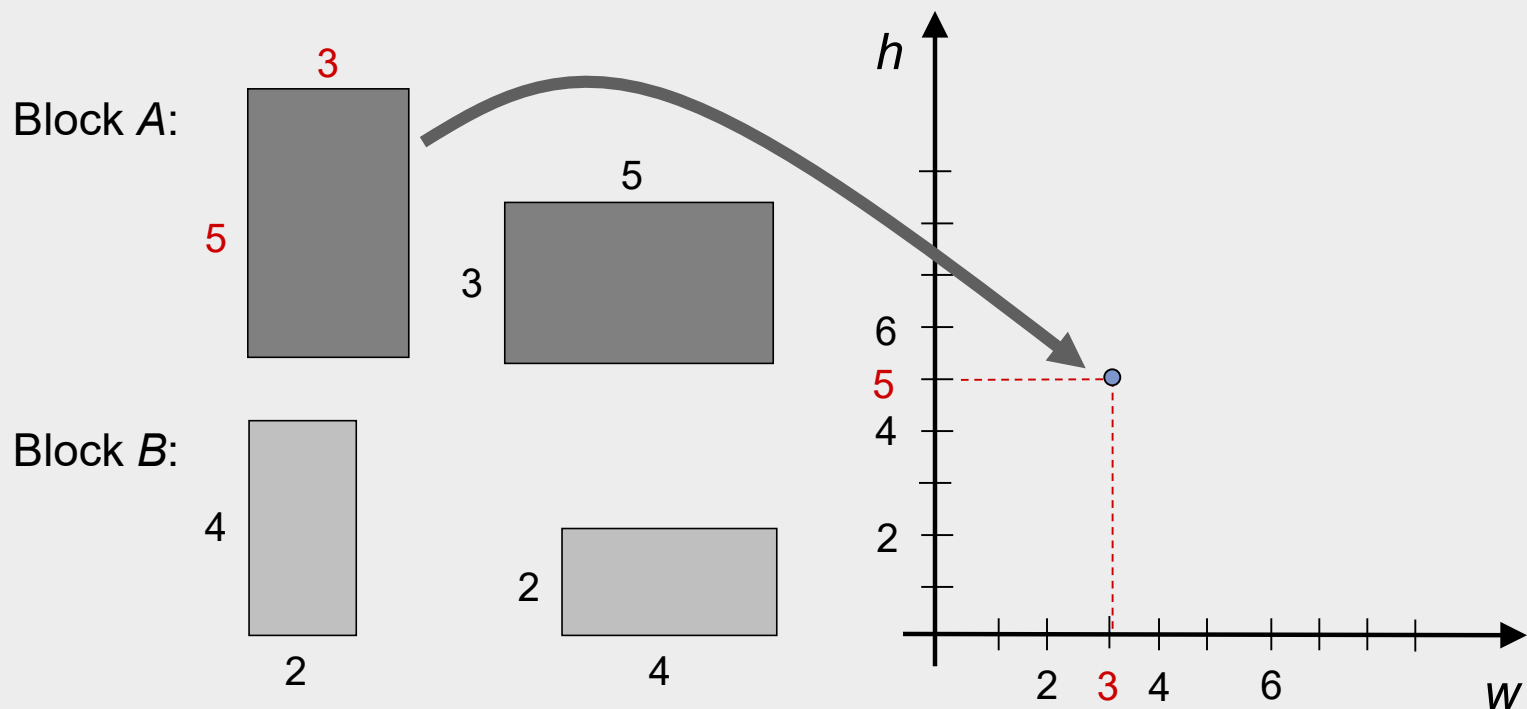
Step 1: Construct the shape functions of the blocks





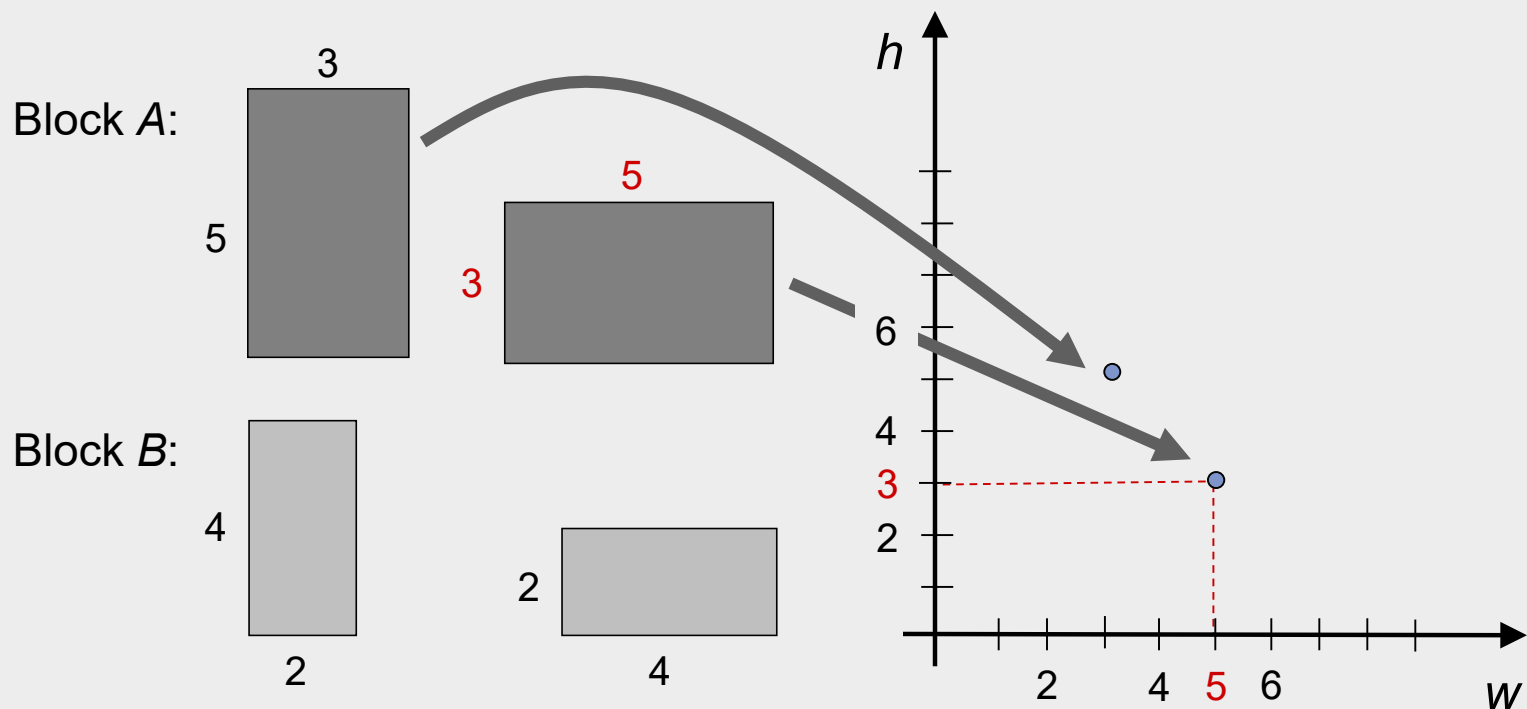
### 3.5.1 Floorplan Sizing – Example

Step 1: Construct the shape functions of the blocks



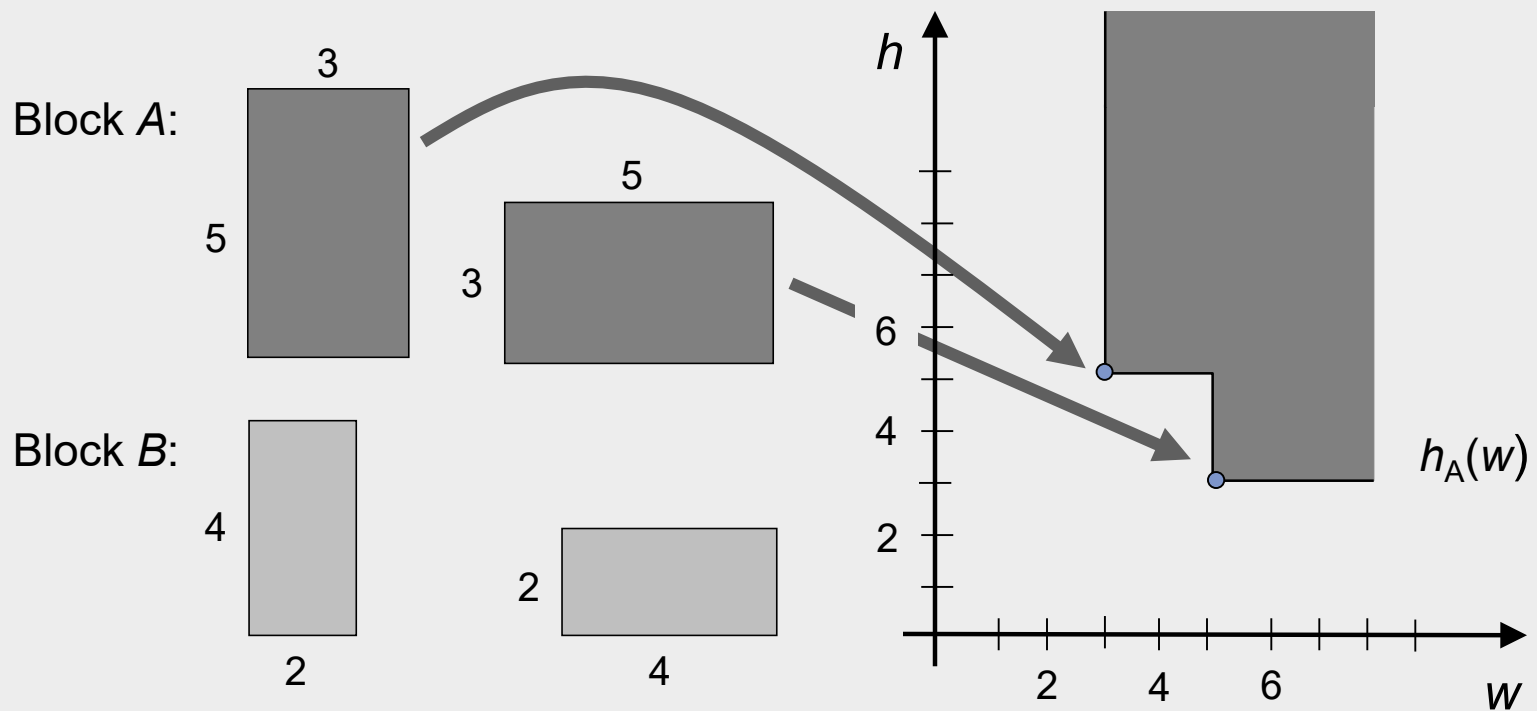
### 3.5.1 Floorplan Sizing – Example

Step 1: Construct the shape functions of the blocks



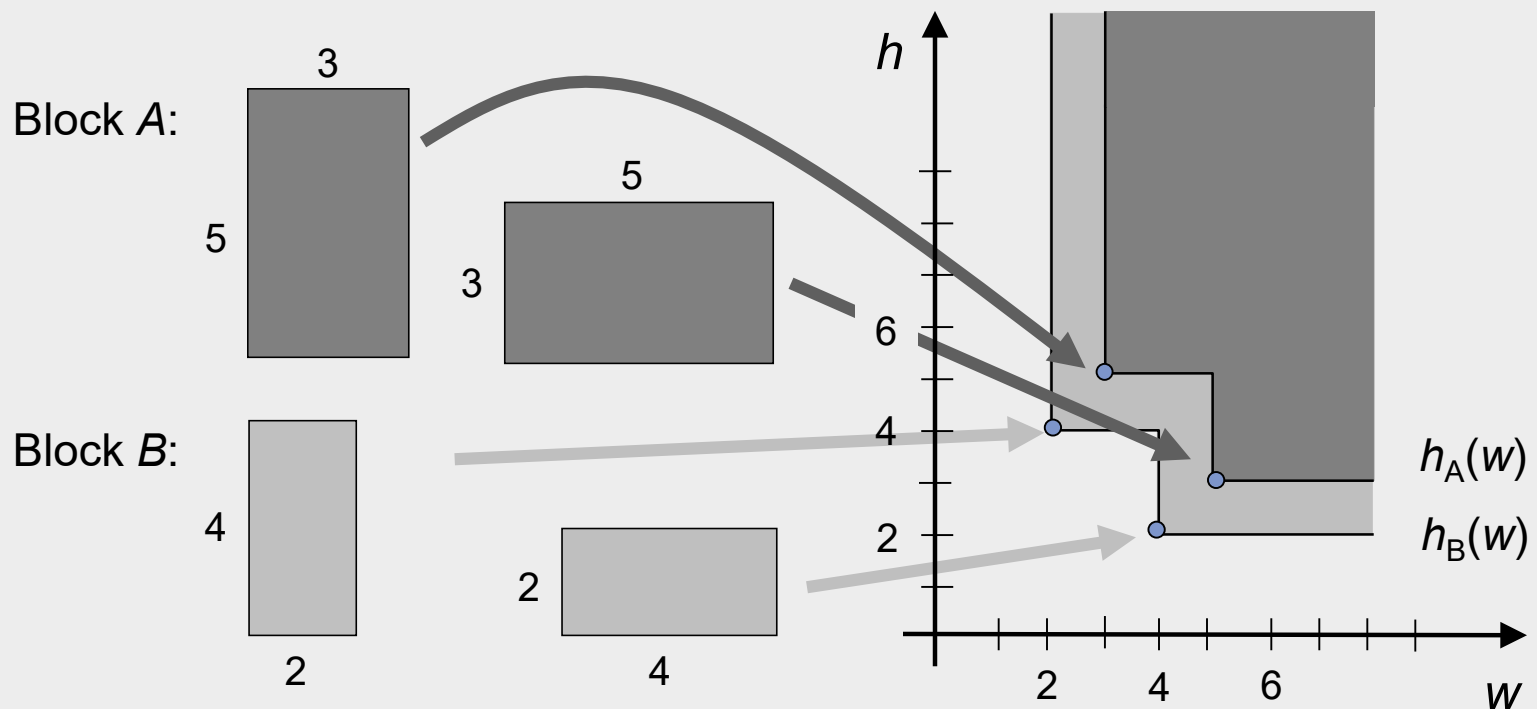
### 3.5.1 Floorplan Sizing – Example

Step 1: Construct the shape functions of the blocks



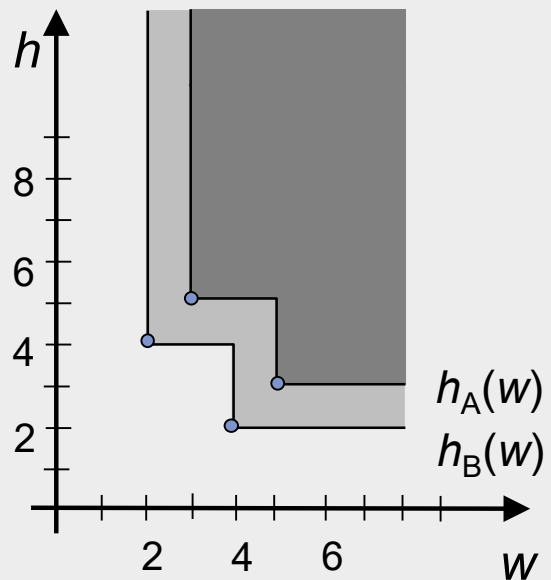
### 3.5.1 Floorplan Sizing – Example

Step 1: Construct the shape functions of the blocks



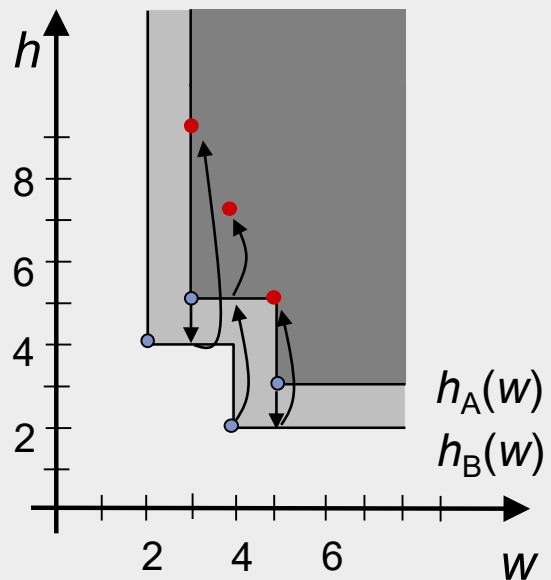
### 3.5.1 Floorplan Sizing – Example

Step 2: Determine the shape function of the top-level floorplan (vertical)



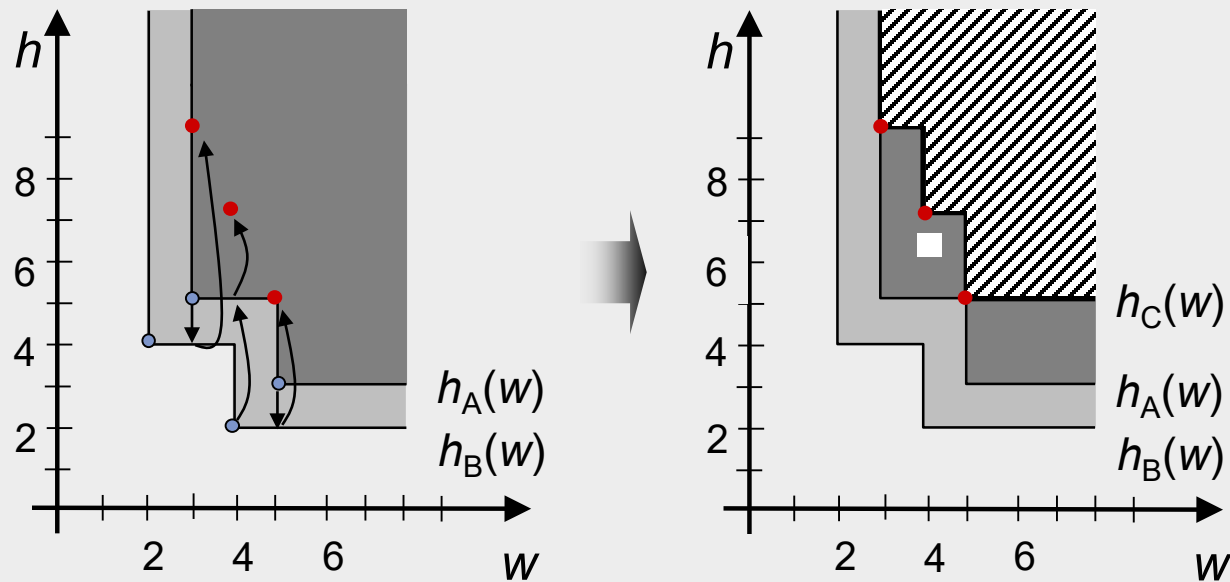
### 3.5.1 Floorplan Sizing – Example

Step 2: Determine the shape function of the top-level floorplan (vertical)



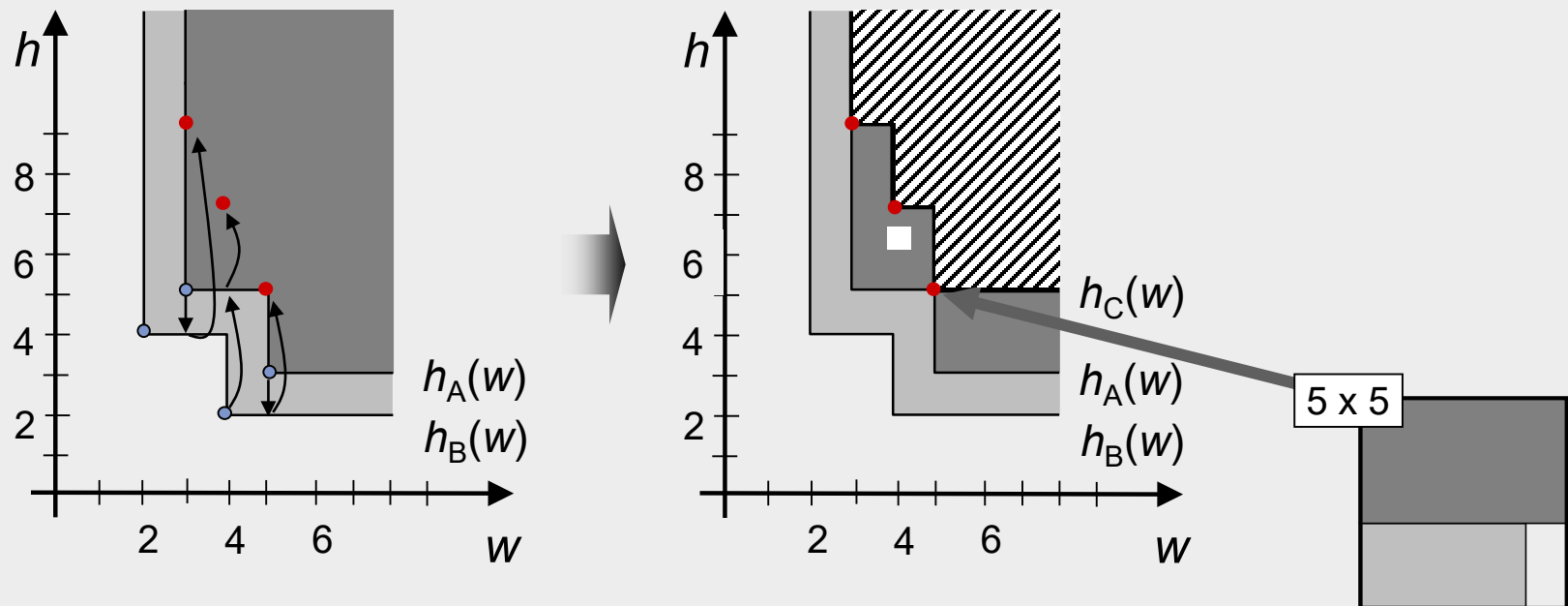
### 3.5.1 Floorplan Sizing – Example

Step 2: Determine the shape function of the top-level floorplan (vertical)



### 3.5.1 Floorplan Sizing – Example

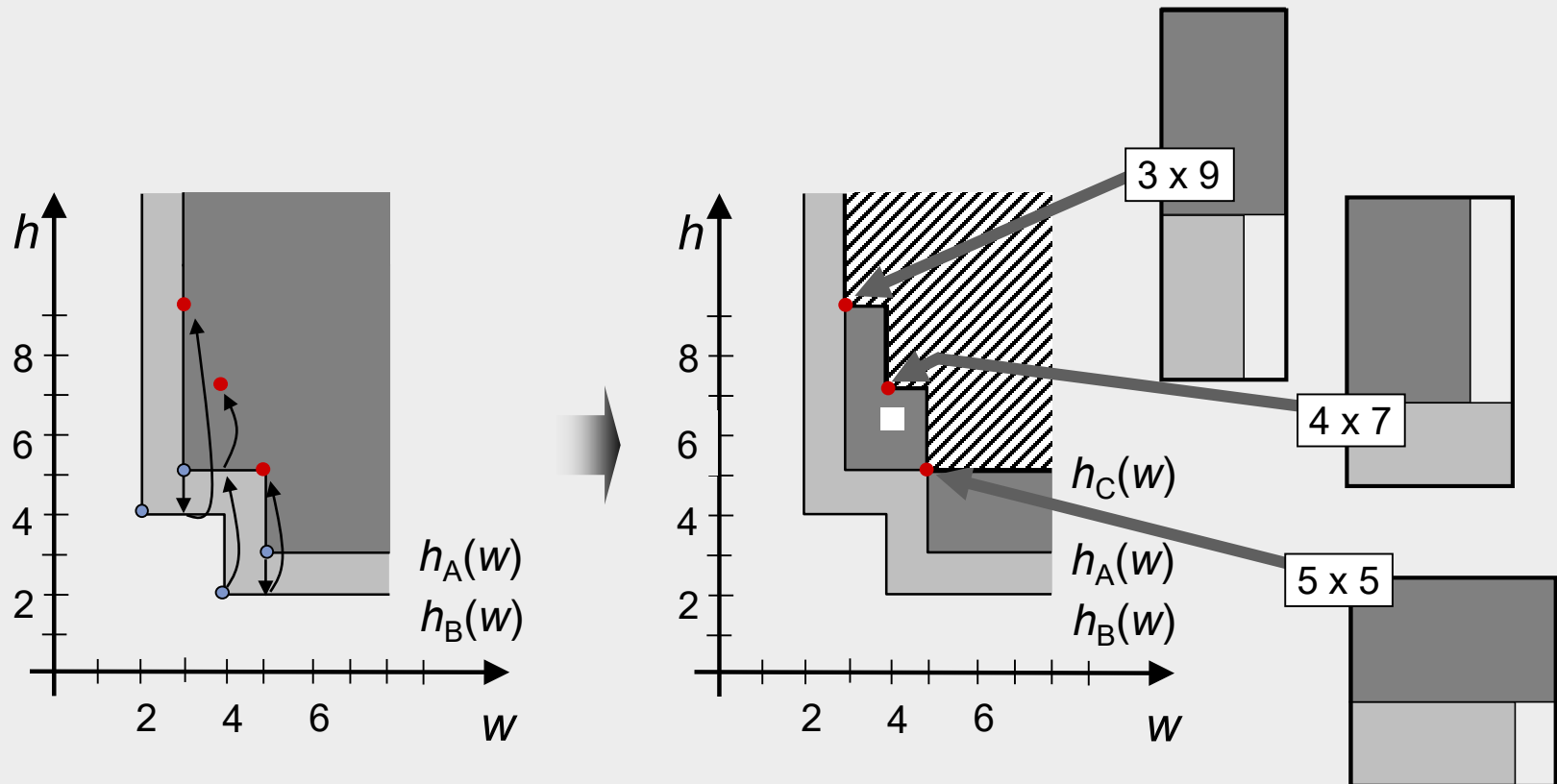
Step 2: Determine the shape function of the top-level floorplan (vertical)





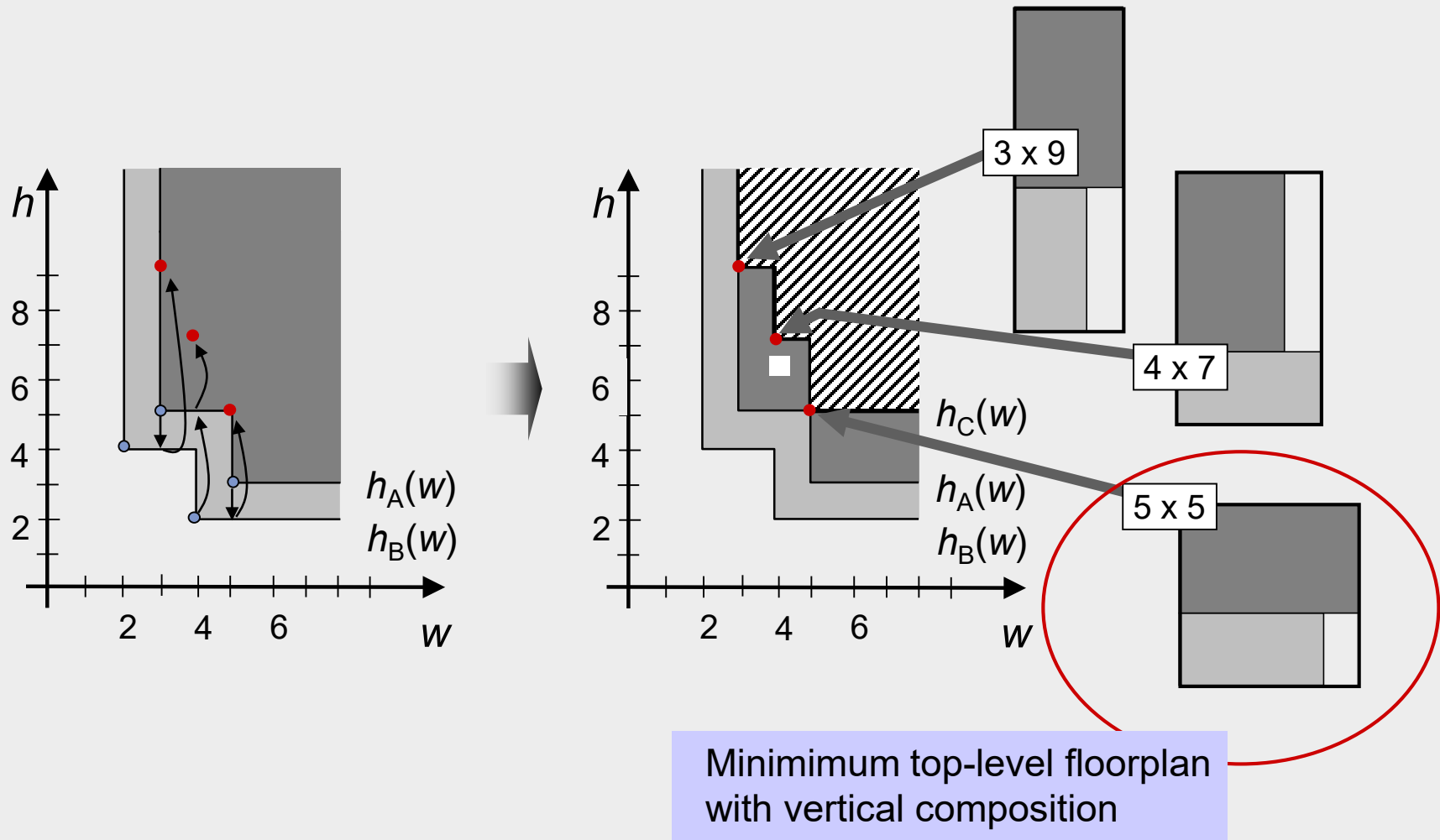
### 3.5.1 Floorplan Sizing – Example

Step 2: Determine the shape function of the top-level floorplan (vertical)



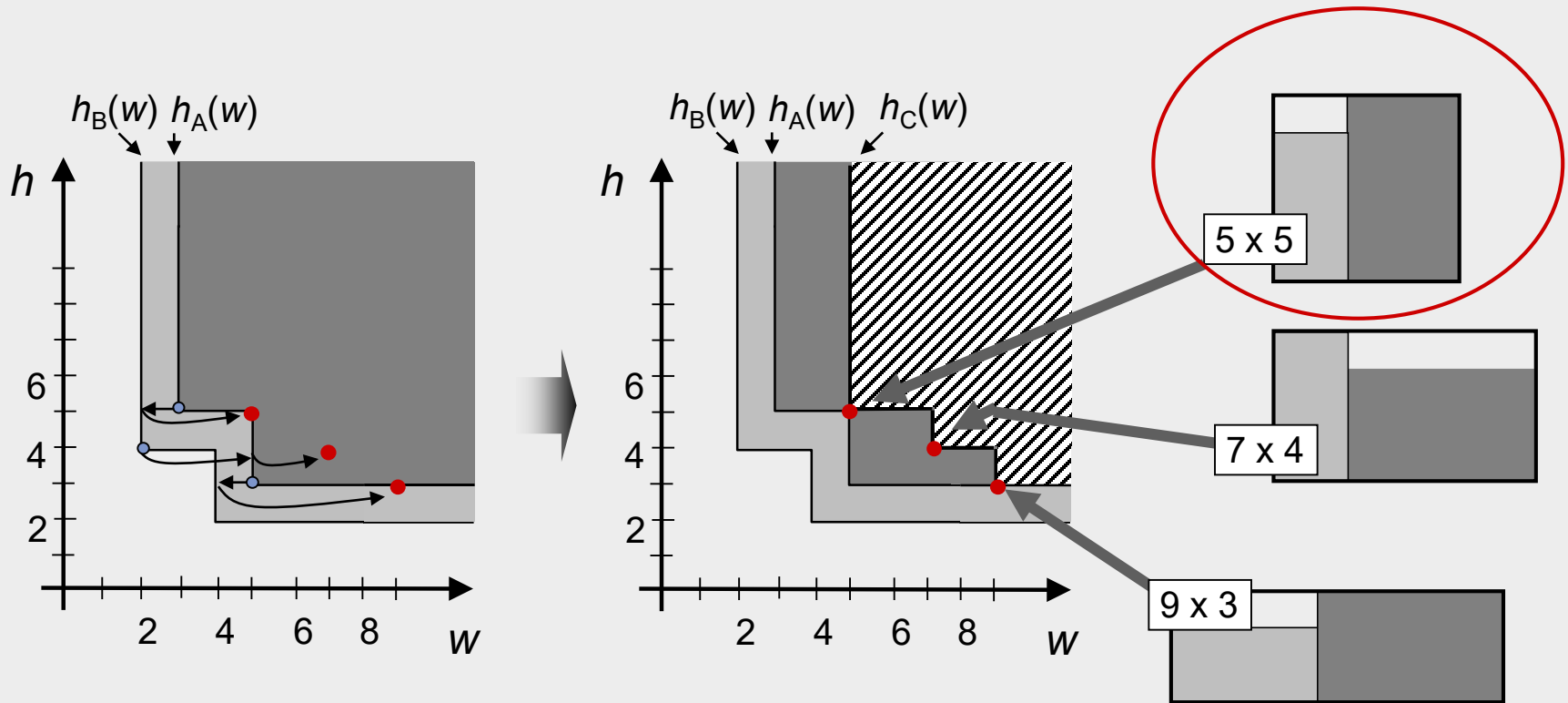
### 3.5.1 Floorplan Sizing – Example

Step 2: Determine the shape function of the top-level floorplan (vertical)



### 3.5.1 Floorplan Sizing – Example

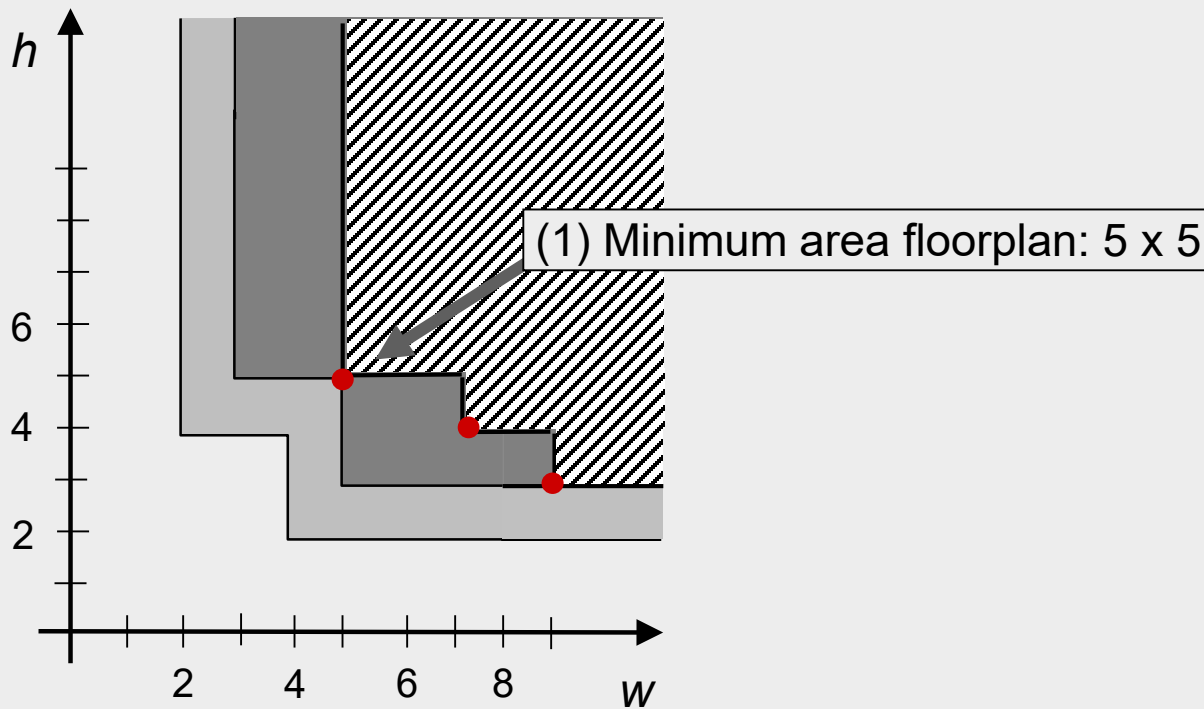
Step 2: Determine the shape function of the top-level floorplan (horizontal)



Minimum top-level floorplan  
with horizontal composition

### 3.5.1 Floorplan Sizing – Example

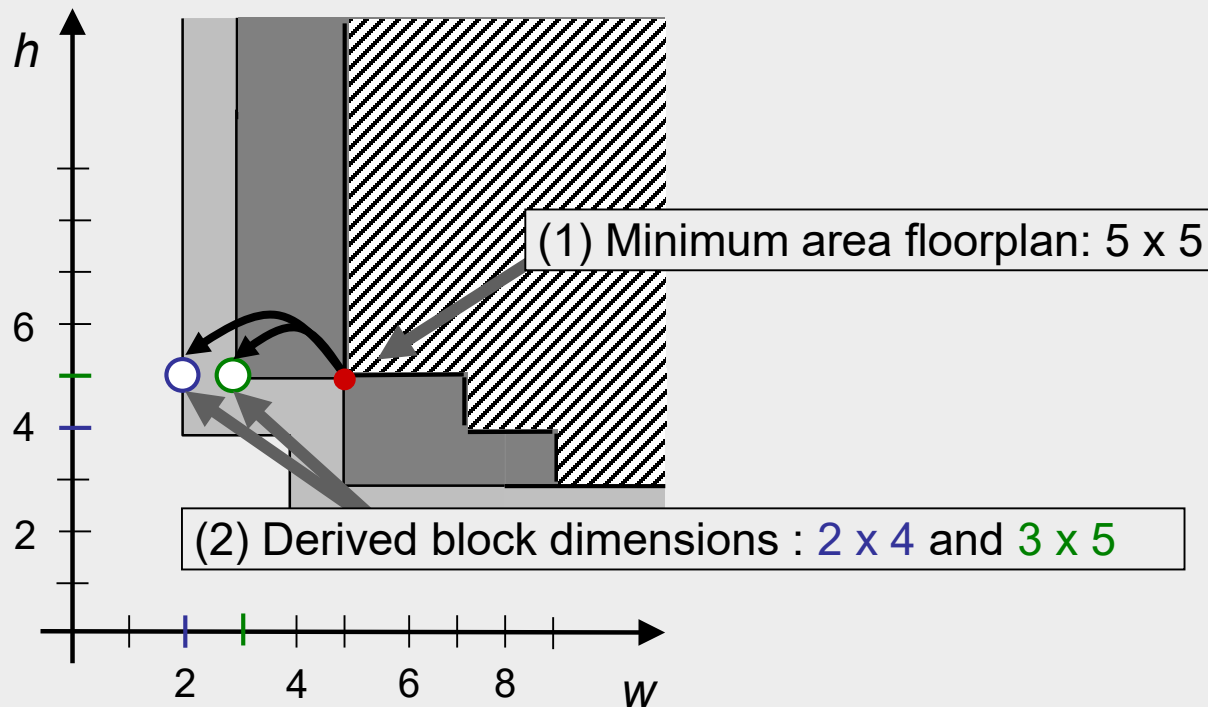
Step 3: Find the individual blocks' dimensions and locations



Horizontal composition

### 3.5.1 Floorplan Sizing – Example

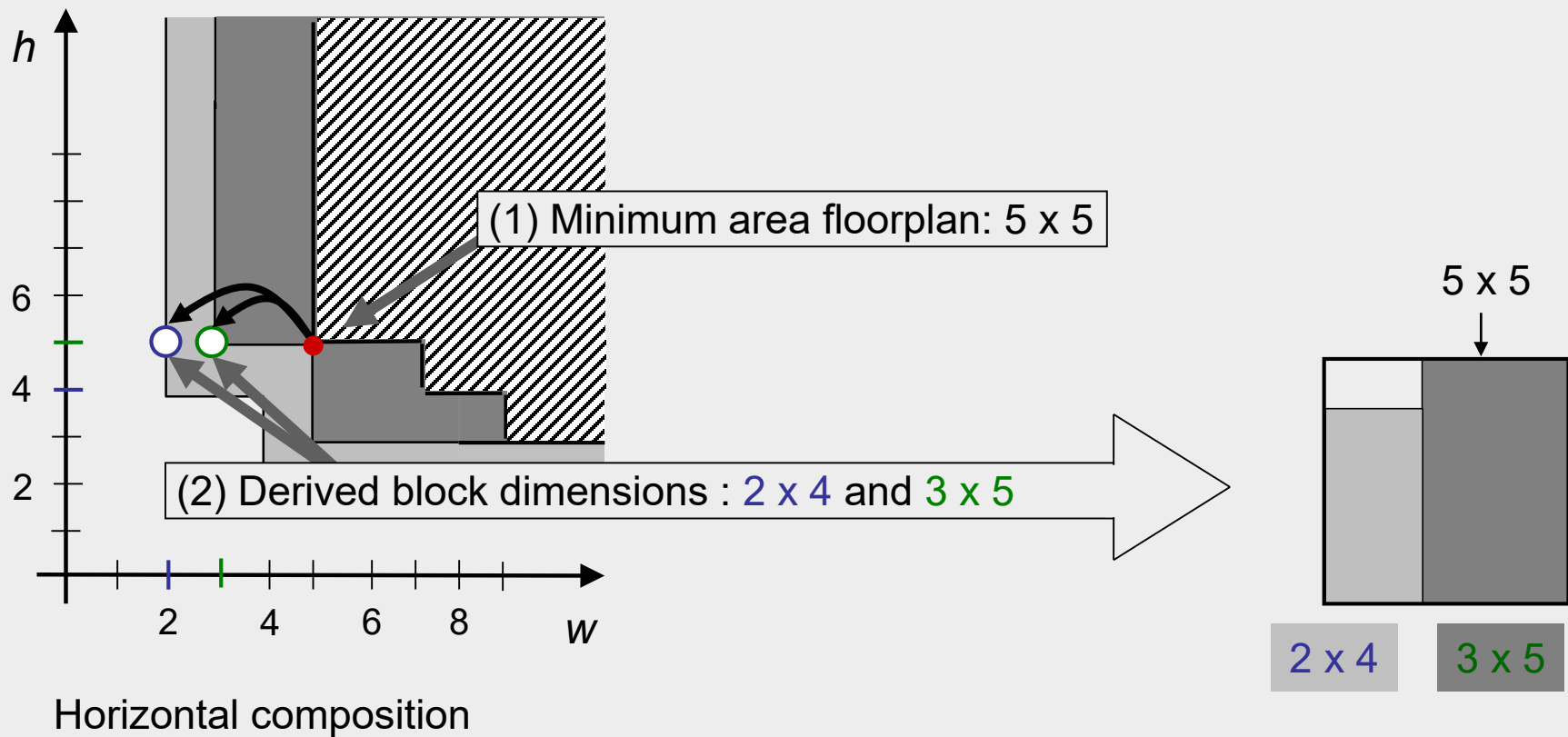
Step 3: Find the individual blocks' dimensions and locations



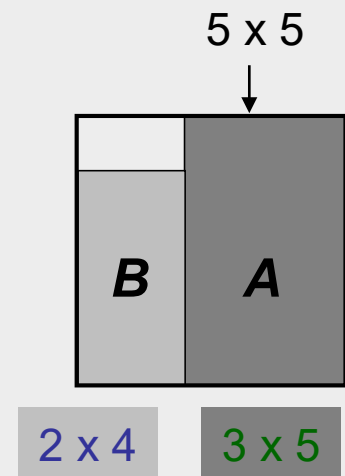
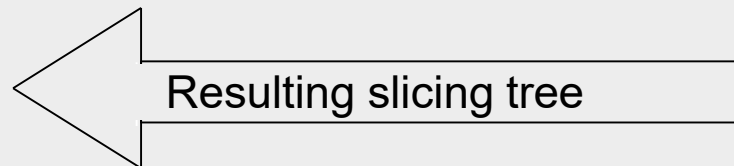
Horizontal composition

### 3.5.1 Floorplan Sizing – Example

Step 3: Find the individual blocks' dimensions and locations

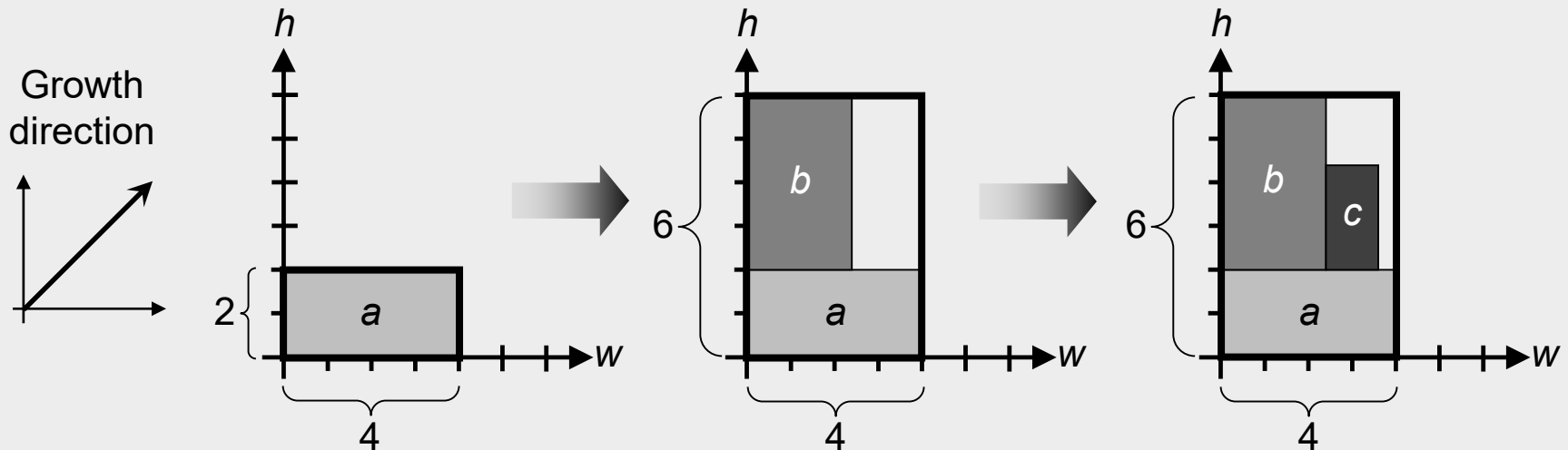


### 3.5.1 Floorplan Sizing – Example



## 3.5.2 Cluster Growth

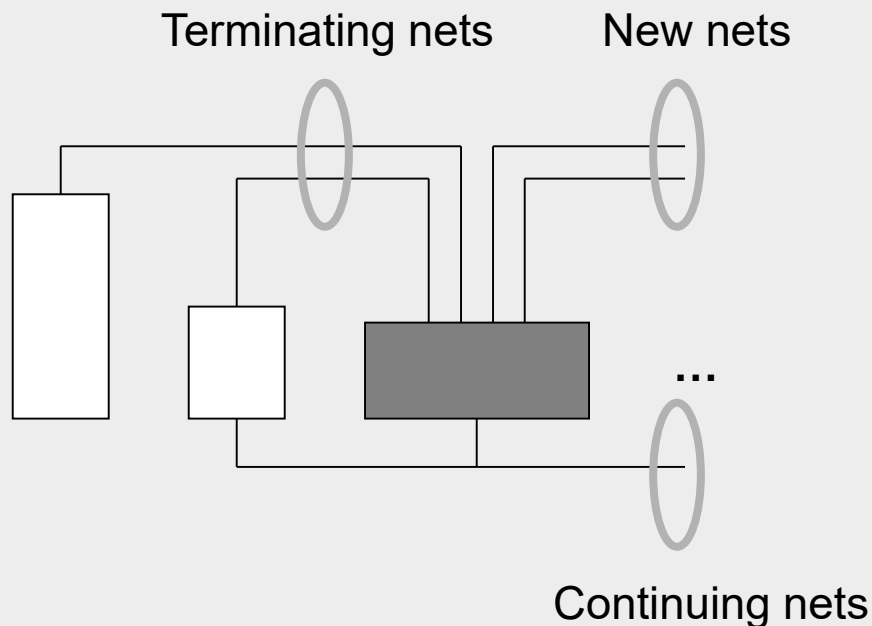
- Iteratively add blocks to the cluster until all blocks are assigned
- Only the different orientations of the blocks instead of the shape / aspect ratio are taken into account
- Linear ordering to minimize total wirelength of connections between blocks





### 3.5.2 Cluster Growth – Linear Ordering

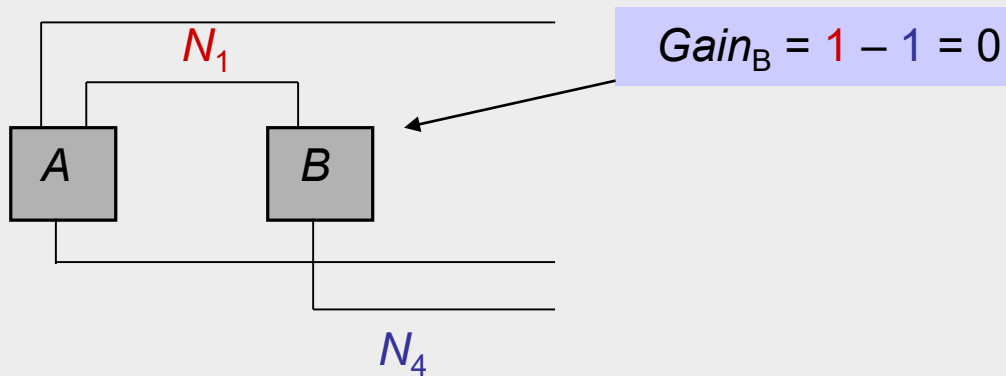
- **New nets** have no pins on any block from the partially-constructed ordering
- **Terminating nets** have no other incident blocks that are unordered
- **Continuing nets** have at least one pin on a block from the partially-constructed ordering and at least one pin on an unordered block



### 3.5.2 Cluster Growth – Linear Ordering

- Gain of each block  $m$  is calculated:

$$Gain_m = (\text{Number of terminating nets of } m) - (\text{New nets of } m)$$

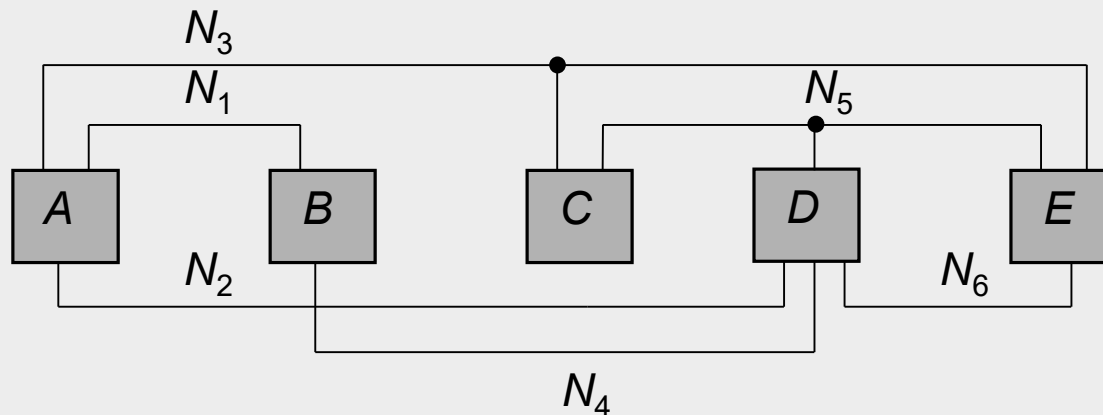


- The block with the maximum gain is selected to be placed next

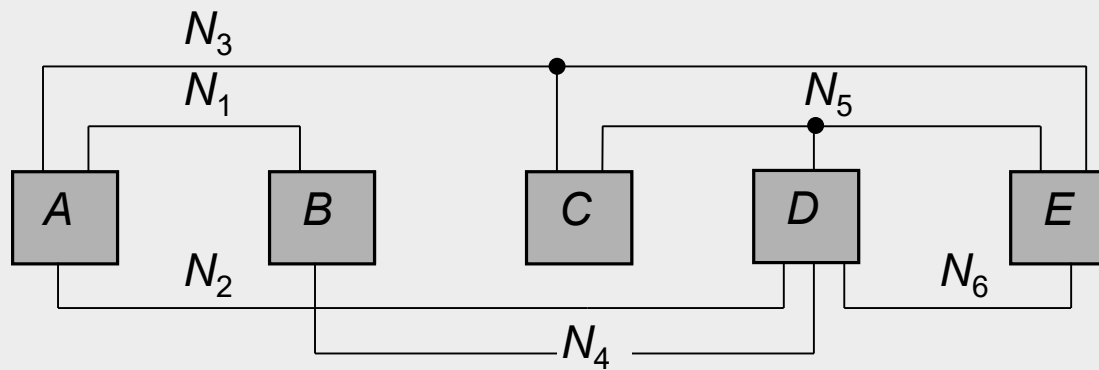
## 3.5.2 Cluster Growth – Linear Ordering (Example)

Given:

- Netlist with five blocks  $A, B, C, D, E$  and six nets  
 $N_1 = \{A, B\}$   
 $N_2 = \{A, D\}$   
 $N_3 = \{A, C, E\}$   
 $N_4 = \{B, D\}$   
 $N_5 = \{C, D, E\}$   
 $N_6 = \{D, E\}$
- Initial block:  $A$



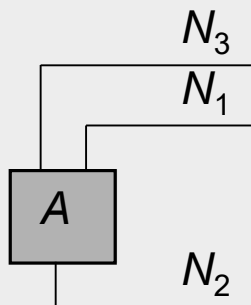
Task: Linear ordering with minimum netlength

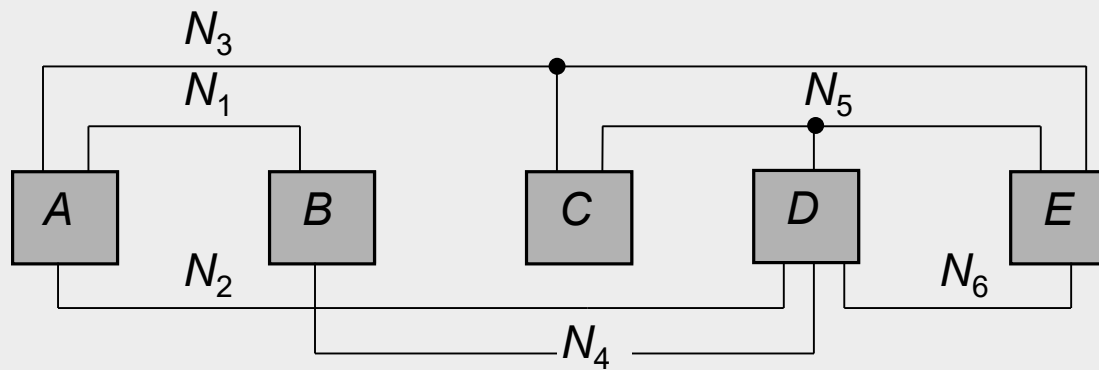


Iteration #	Block	New Nets	Terminating Nets	Gain	Continuing Nets
0	<b>A</b>	$N_1, N_2, N_3$	--	-3	--

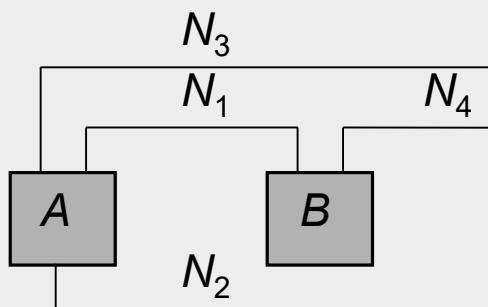
Initial block

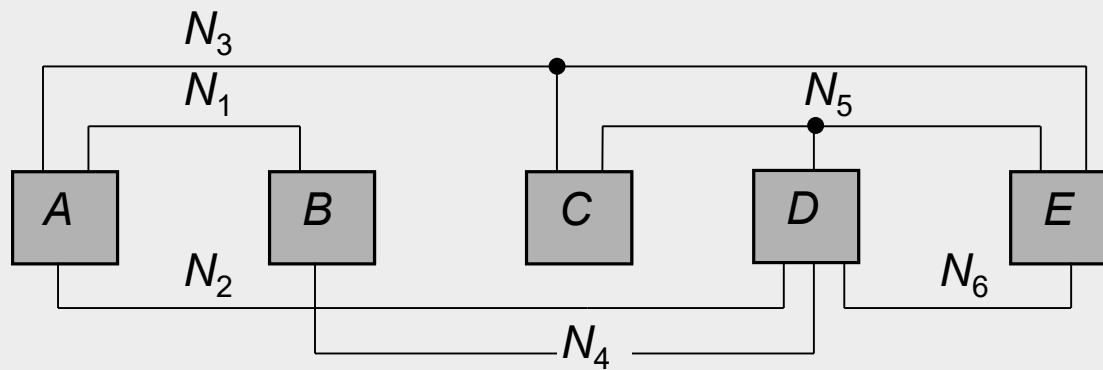
$Gain_A = (\text{Number of terminating nets of } A) - (\text{New nets of } A)$



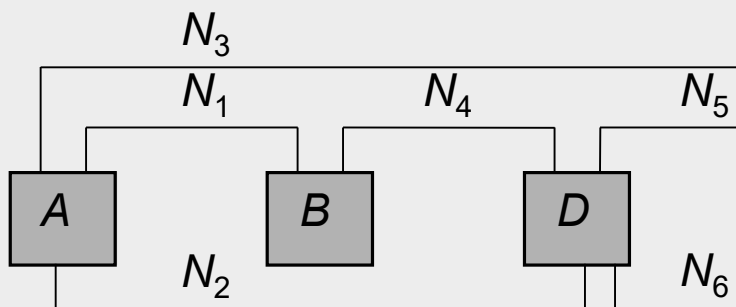


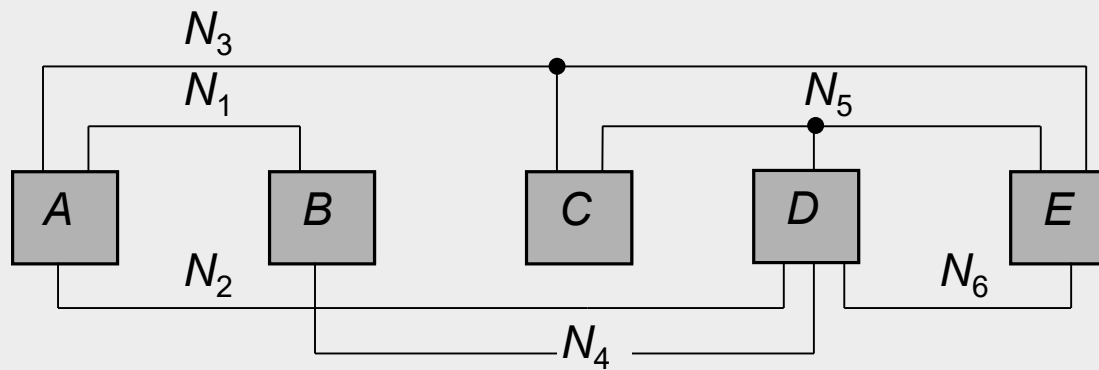
Iteration #	Block	New Nets	Terminating Nets	Gain	Continuing Nets
0	<b>A</b>	$N_1, N_2, N_3$	--	-3	--
1	<b>B</b>	$N_4$	$N_1$	0	--
	<b>C</b>	$N_5$	--	-1	$N_3$
	<b>D</b>	$N_4, N_5, N_6$	$N_2$	-2	--
	<b>E</b>	$N_5, N_6$	--	-2	$N_3$





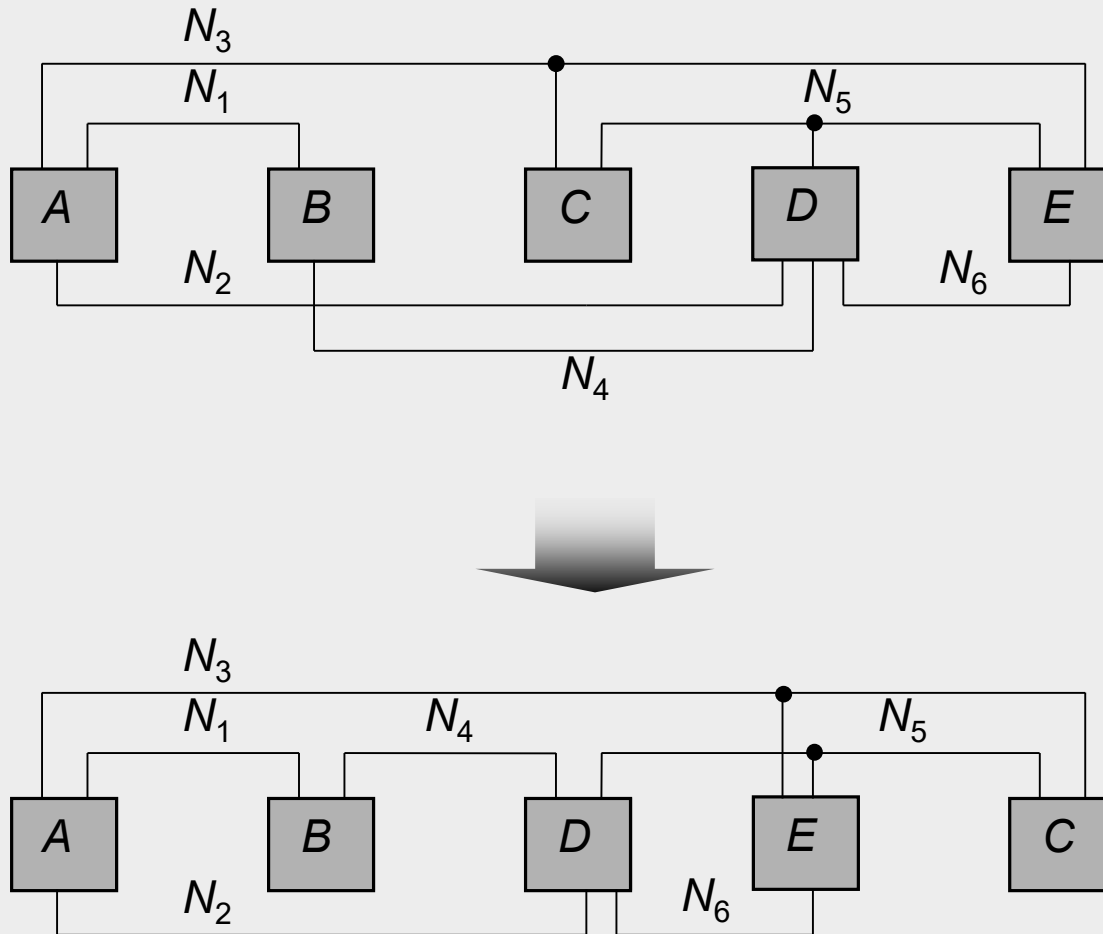
Iteration #	Block	New Nets	Terminating Nets	Gain	Continuing Nets
0	<b>A</b>	$N_1, N_2, N_3$	--	-3	--
1	<b>B</b>	$N_4$	$N_1$	0	--
	<b>C</b>	$N_5$	--	-1	$N_3$
	<b>D</b>	$N_4, N_5, N_6$	$N_2$	-2	--
	<b>E</b>	$N_5, N_6$	--	-2	$N_3$
2	<b>C</b>	$N_5$	--	-1	$N_3$
	<b>D</b>	$N_5, N_6$	$N_2, N_4$	0	--
	<b>E</b>	$N_5, N_6$	--	-2	$N_3$





Iteration #	Block	New Nets	Terminating Nets	Gain	Continuing Nets
0	<b>A</b>	$N_1, N_2, N_3$	--	-3	--
1	<b>B</b>	$N_4$	$N_1$	0	--
	<b>C</b>	$N_5$	--	-1	$N_3$
	<b>D</b>	$N_4, N_5, N_6$	$N_2$	-2	--
	<b>E</b>	$N_5, N_6$	--	-2	$N_3$
2	<b>C</b>	$N_5$	--	-1	$N_3$
	<b>D</b>	$N_5, N_6$	$N_2, N_4$	0	--
	<b>E</b>	$N_5, N_6$	--	-2	$N_3$
3	<b>C</b>	--	--	0	$N_3, N_5$
	<b>E</b>	--	$N_6$	1	$N_3, N_5$
4	<b>C</b>	--	$N_3, N_5$	2	--

### 3.5.2 Cluster Growth – Linear Ordering (Example)





## 3.5.2 Cluster Growth – Algorithm

**Input:** set of all blocks  $M$ , cost function  $C$

**Output:** optimized floorplan  $F$  based on  $C$

$F = \emptyset$

$order = \text{LINEAR\_ORDERING}(M)$

// generate linear ordering

**for** ( $i = 1$  **to**  $|order|$ )

$curr\_block = order[i]$

$\text{ADD\_TO\_FLOORPLAN}(F, curr\_block, C)$

// find location and orientation  
// of  $curr\_block$  that causes  
// smallest increase based on  
//  $C$  while obeying constraints

### Analysis

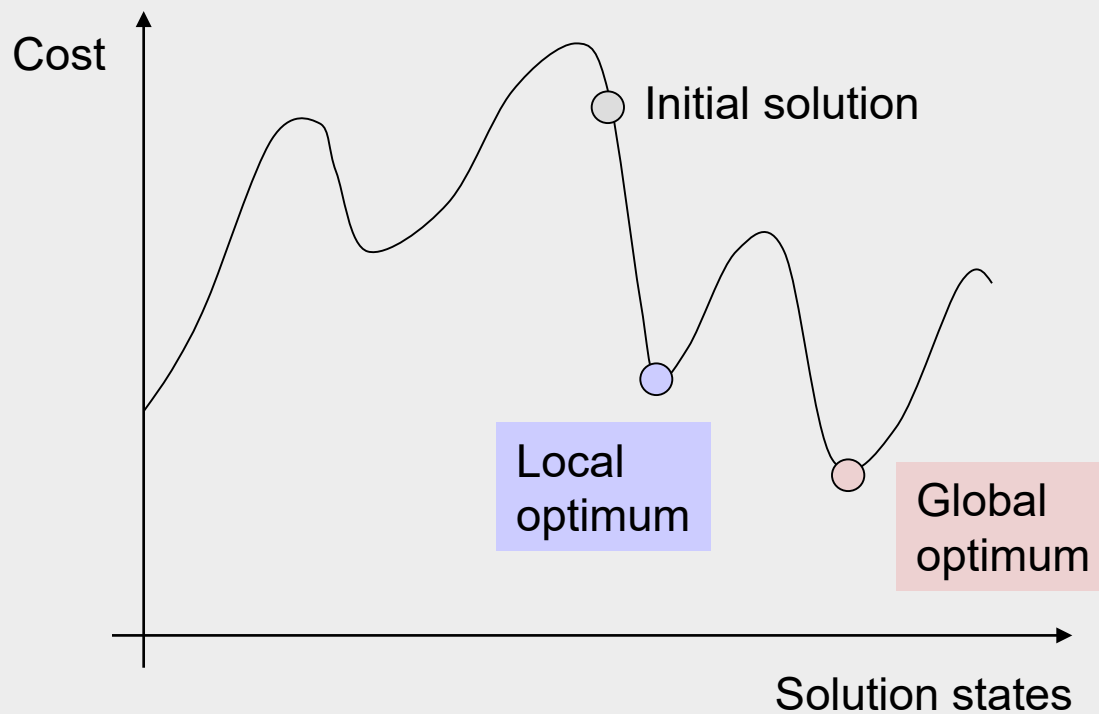
- The objective is to minimize the total wirelength of connections blocks
- Though this produces mediocre solutions, the algorithm is easy to implement and fast.
- Can be used to find the initial floorplan solutions for iterative algorithms such as *simulated annealing*.

### 3.5.3 Simulated Annealing

#### Introduction

- Simulated Annealing (SA) algorithms are iterative in nature.
- Begins with an initial (arbitrary) solution and seeks to incrementally improve the objective function.
- During each iteration, a **local** neighborhood of the current solution is considered. A new candidate solution is formed by a **small perturbation** of the current solution.
- Unlike greedy algorithms, SA algorithms **can accept** candidate solutions with **higher cost**.

### 3.5.3 Simulated Annealing



### 3.5.3 Simulated Annealing

#### What is annealing?

- Definition (from material science): controlled cooling process of high-temperature materials to modify their properties.
- Cooling changes material structure from being highly randomized (chaotic) to being structured (stable).
- The way that atoms settle in low-temperature state is probabilistic in nature.
- Slower cooling has a higher probability of achieving a **perfect lattice** with minimum-energy
  - Cooling process occurs in steps
  - Atoms need enough time to try different structures
  - Sometimes, atoms may move across larger distances and create (intermediate) higher-energy states
  - Probability of the accepting higher-energy states decreases with temperature

### 3.5.3 Simulated Annealing

#### Simulated Annealing

- Generate an initial solution  $S_{init}$ , and evaluate its cost.
- Generate a new solution  $S_{new}$  by performing a random walk
- $S_{new}$  is accepted or rejected based on the temperature  $T$ 
  - Higher  $T$  means a higher probability to accept  $S_{new}$  if  $COST(S_{new}) > COST(S_{init})$
  - $T$  slowly decreases to form the final solution
- Boltzmann acceptance criterion, where  $r$  is a random number  $[0,1)$

$$e^{\frac{COST(S_{init}) - COST(S_{new})}{T}} > r$$

### 3.5.3 Simulated Annealing

#### Simulated Annealing

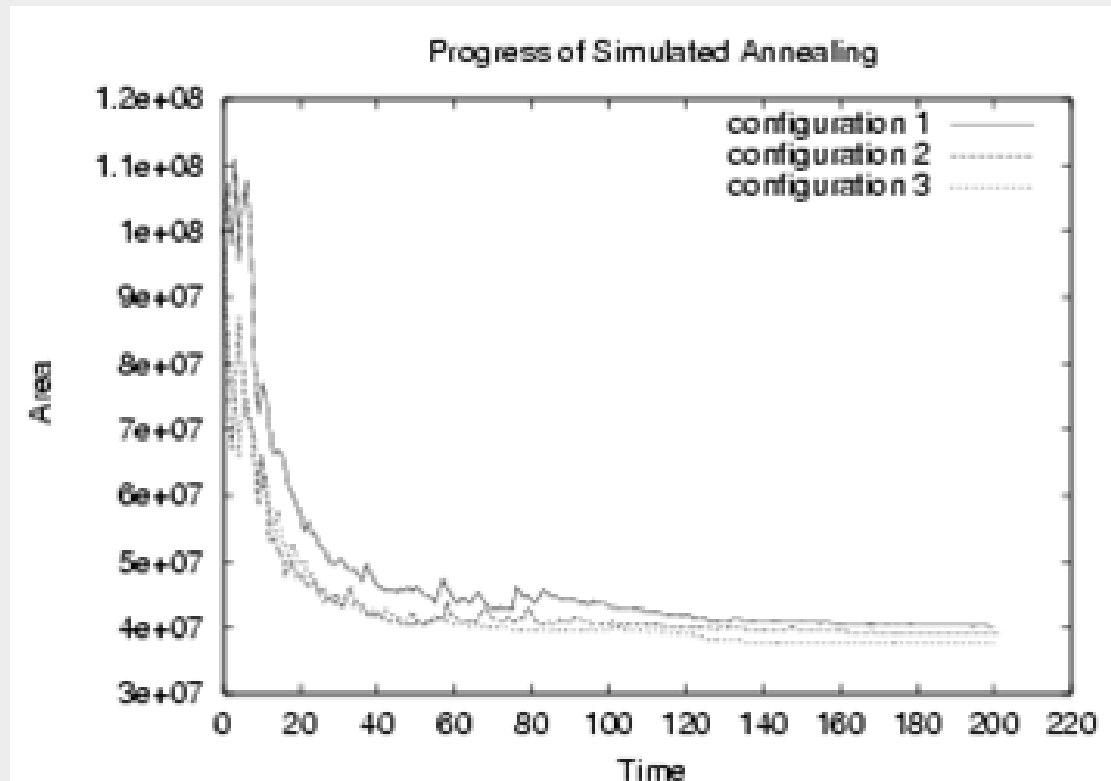
- Generate an initial solution and evaluate its cost
- Generate a new solution by performing a random walk
- Solution is accepted or rejected based on a temperature parameter  $T$
- Higher  $T$  indicates higher probability to accept a solution with higher cost
- $T$  slowly decreases to form the finalized solution.

- Boltzmann acceptance criterion:

$$e^{-\frac{\text{cost}(\text{curr}_{sol}) - \text{cost}(\text{next}_{sol})}{T}} > r$$

$\text{curr}_{sol}$ : current solution  
 $\text{next}_{sol}$ : new solution after perturbation  
 $T$ : current temperature  
 $r$ : random number between  $[0,1)$  from normal distr.

### 3.5.3 Simulated Annealing – Algorithm






### 3.5.3 Simulated Annealing – Algorithm

**Input:** initial solution *init\_sol*

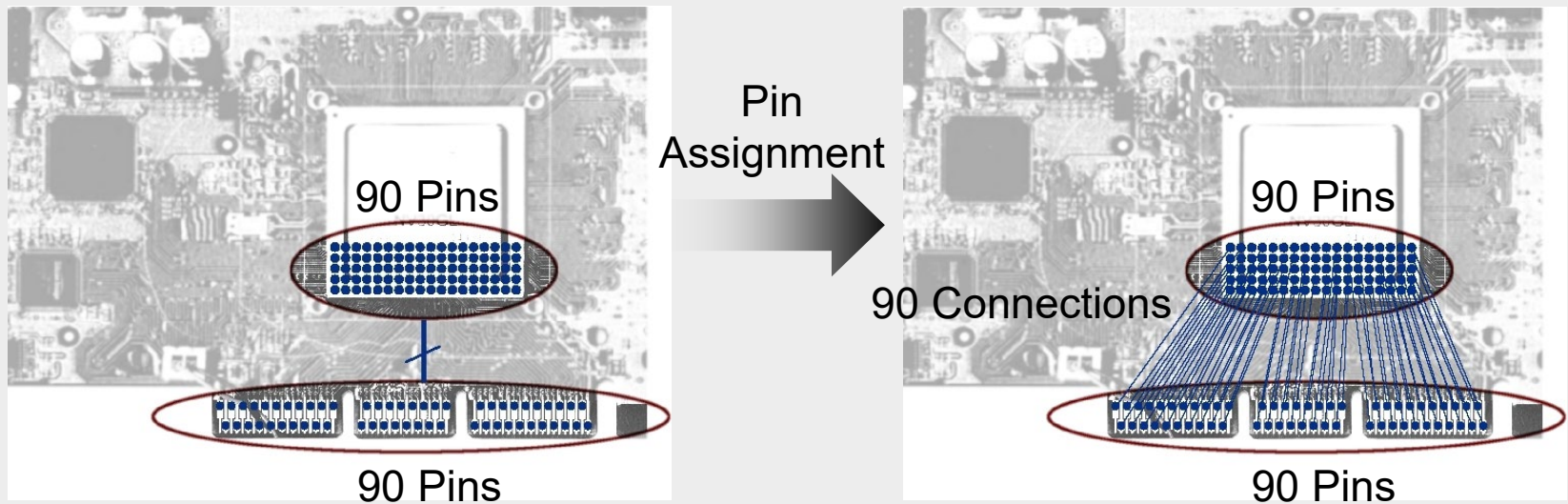
**Output:** optimized new solution *curr\_sol*

```
T = T0                                     // initialization
i = 0
curr_sol = init_sol
curr_cost = COST(curr_sol)
while (T > Tmin)
    while (stopping criterion is not met)
        i = i + 1
        (ai, bi) = SELECT_PAIR(curr_sol)           // select two objects to perturb
        trial_sol = TRY_MOVE(ai, bi)              // try small local change
        trial_cost = COST(trial_sol)
         $\Delta cost = trial\_cost - curr\_cost$ 
        if ( $\Delta cost < 0$ )                          // if there is improvement,
            curr_cost = trial_cost                  // update the cost and
            curr_sol = MOVE(ai, bi)              // execute the move
        else
            r = RANDOM(0,1)                          // random number [0,1]
            if (r <  $e^{-\Delta cost/T}$ )                // if it meets threshold,
                curr_cost = trial_cost              // update the cost and
                curr_sol = MOVE(ai, bi)          // execute the move
            T =  $\alpha \cdot T$                         // 0 <  $\alpha$  < 1, T reduction
```

- 3.1 Introduction to Floorplanning
- 3.2 Optimization Goals in Floorplanning
- 3.3 Terminology
- 3.4 Floorplan Representations
  - 3.4.1 Floorplan to a Constraint-Graph Pair
  - 3.4.2 Floorplan to a Sequence Pair
  - 3.4.3 Sequence Pair to a Floorplan
- 3.5 Floorplanning Algorithms
  - 3.5.1 Floorplan Sizing
  - 3.5.2 Cluster Growth
  - 3.5.3 Simulated Annealing
  - 3.5.4 Integrated Floorplanning Algorithms
-  **3.6 Pin Assignment**
- 3.7 Power and Ground Routing
  - 3.7.1 Design of a Power-Ground Distribution Network
  - 3.7.2 Planar Routing
  - 3.7.3 Mesh Routing

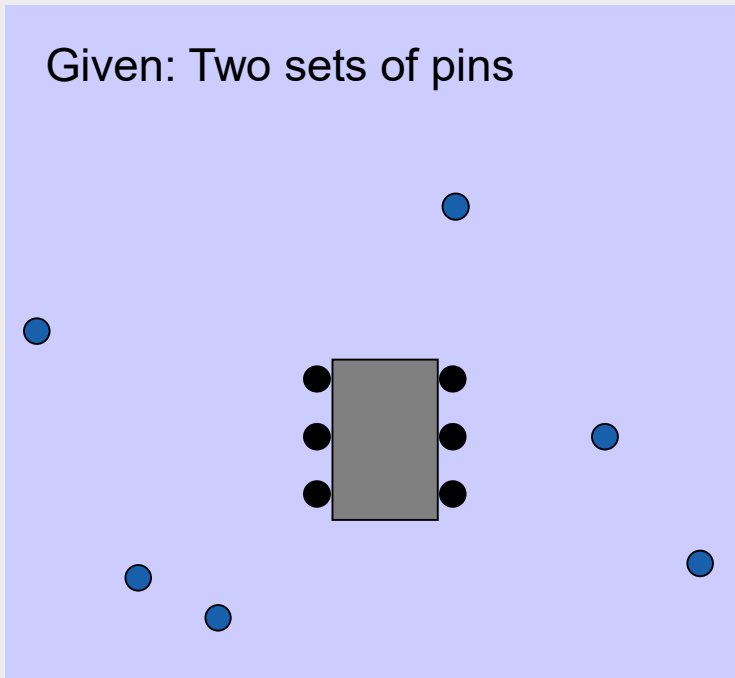
## 3.6 Pin Assignment

During pin assignment, all nets (signals) are assigned to unique pin locations such that the overall design performance is optimized.

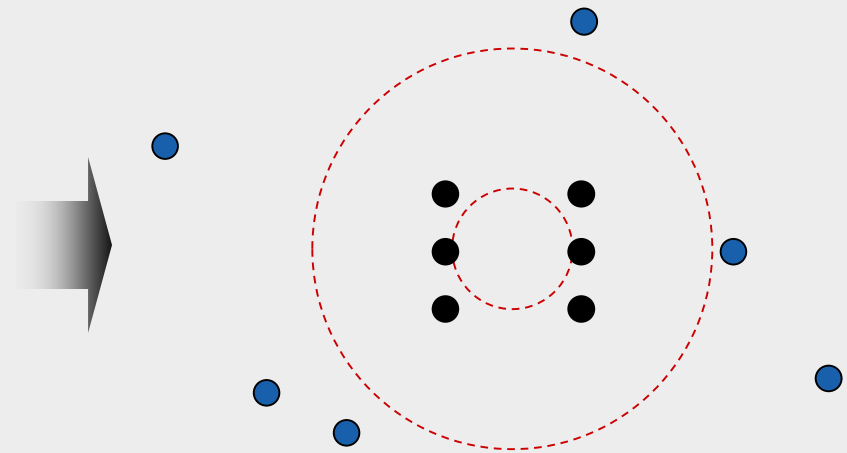


## 3.6 Pin Assignment – Example

Given: Two sets of pins

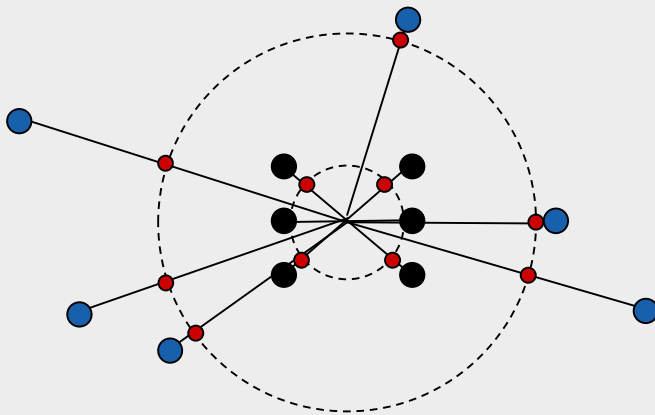


(1) Determine the circles



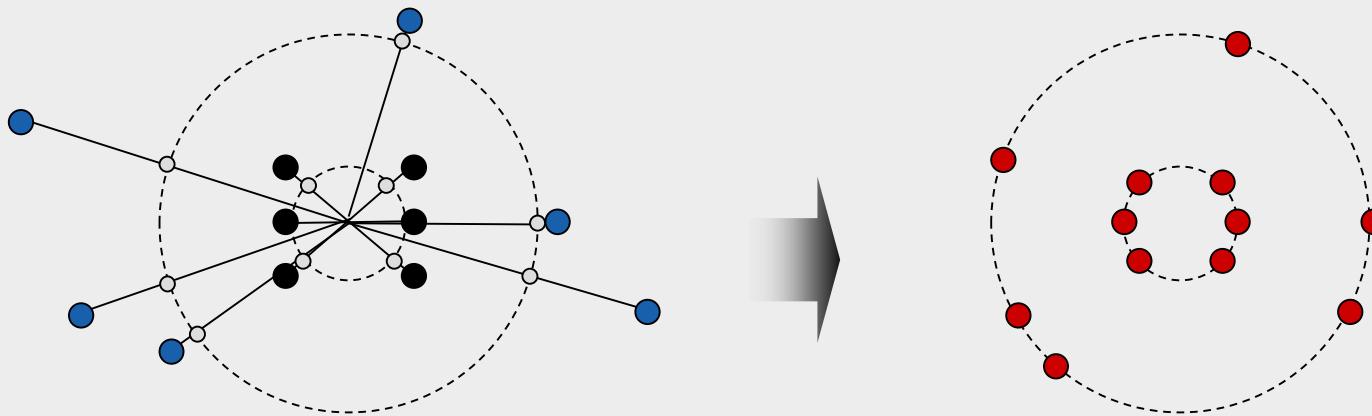
## 3.6 Pin Assignment – Example

(2) Determine the points



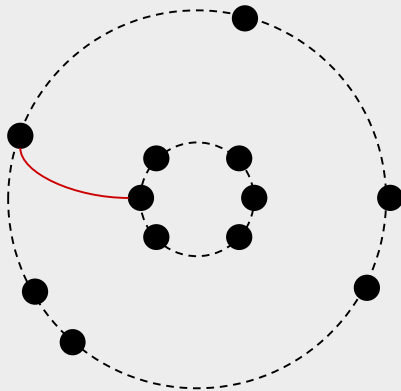
## 3.6 Pin Assignment – Example

(2) Determine the points



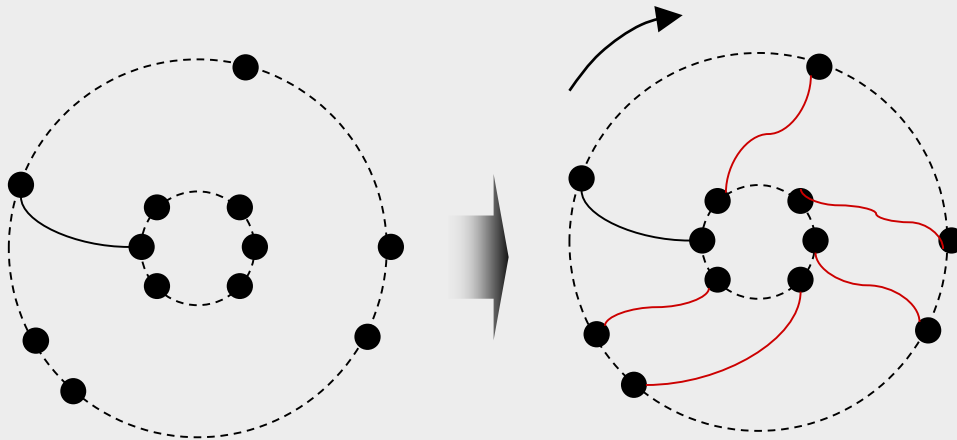
## 3.6 Pin Assignment – Example

(3) Determine initial mapping



## 3.6 Pin Assignment – Example

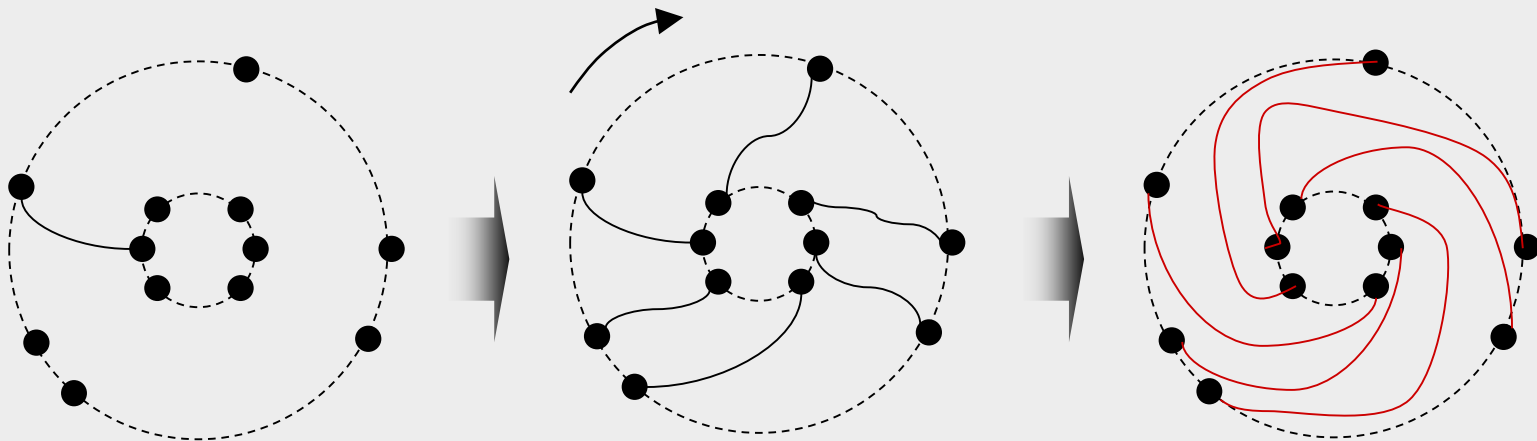
(3) Determine initial mapping and (4) optimize the mapping (complete rotation)





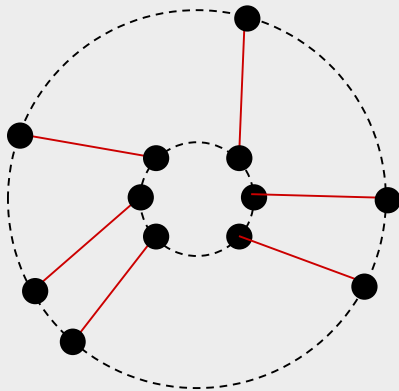
## 3.6 Pin Assignment – Example

(3) Determine initial mapping and (4) optimize the mapping (complete rotation)



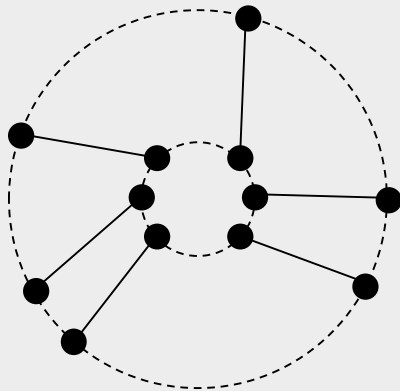
## 3.6 Pin Assignment – Example

(4) Best mapping (shortest Euclidean distance)

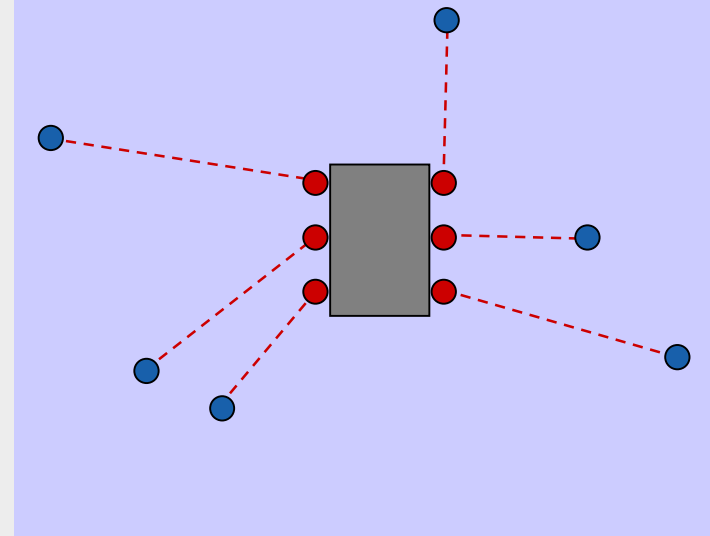


## 3.6 Pin Assignment – Example

(4) Best mapping

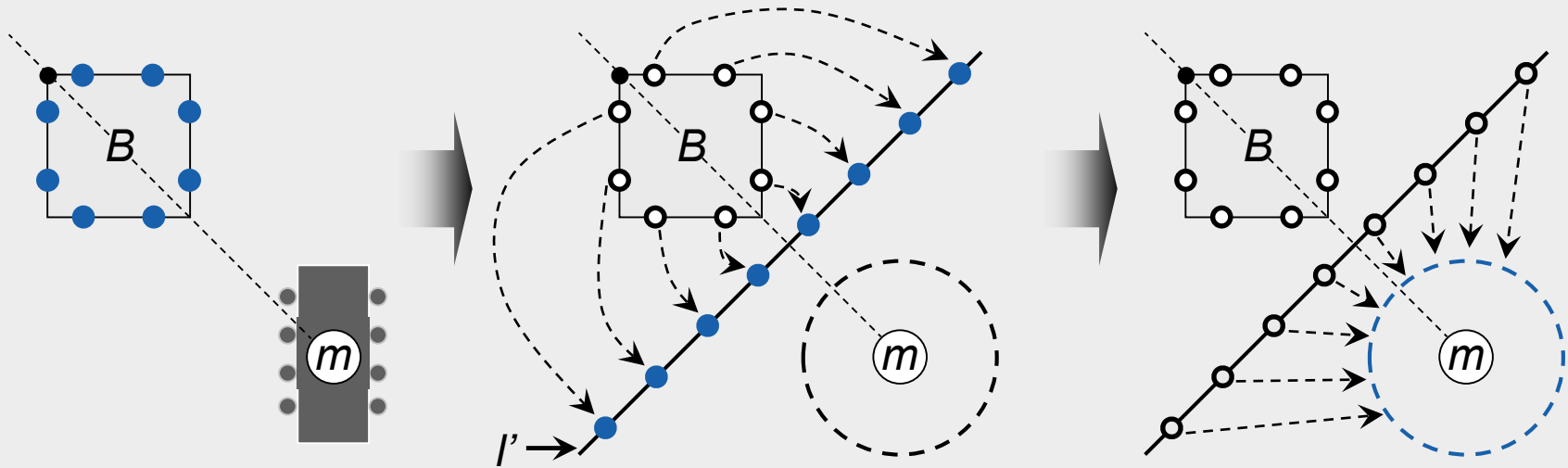


Final pin assignment



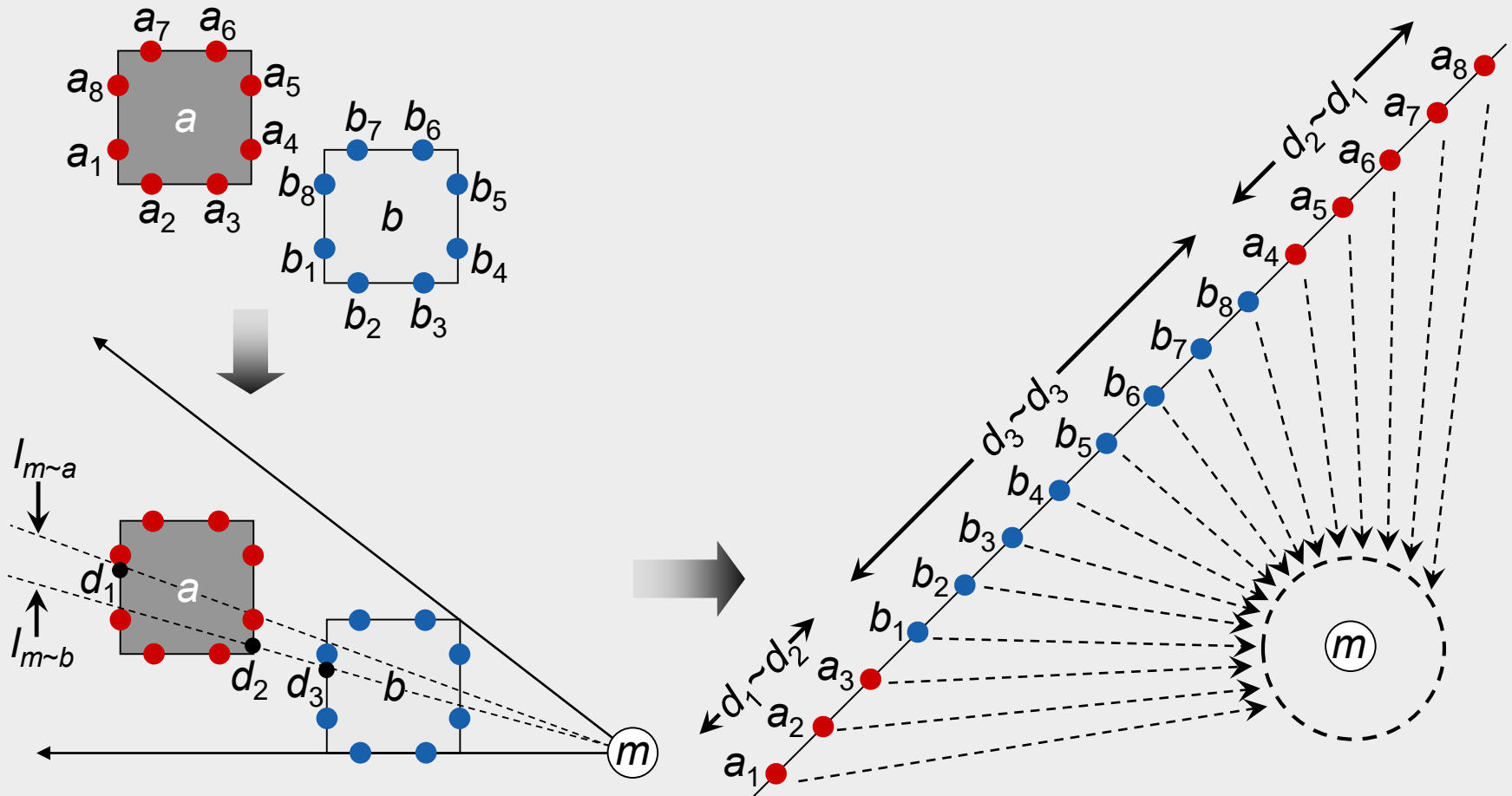
## 3.6 Pin Assignment

Pin assignment to an external block  $B$




## 3.6 Pin Assignment

Pin assignment to two external blocks A and B



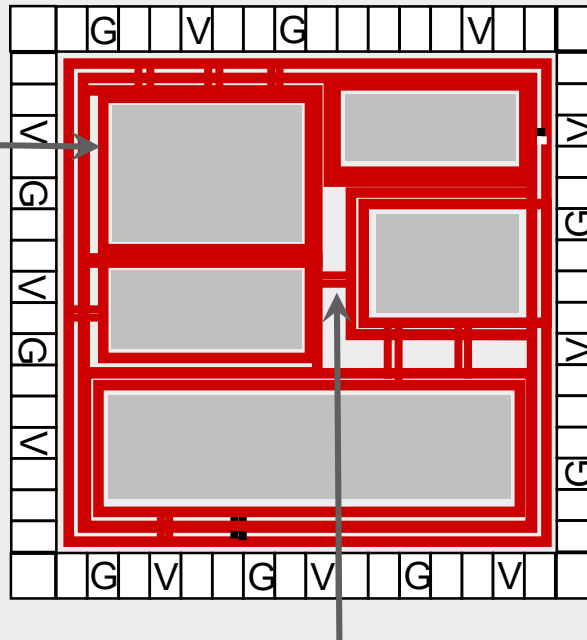
## 3.7 Power and Ground Routing

- 3.1 Introduction to Floorplanning
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  - 3.7.1 Design of a Power-Ground Distribution Network**
  - 3.7.2 Planar Routing**
  - 3.7.3 Mesh Routing**

## 3.7 Power and Ground Routing

### Power-ground distribution for a chip floorplan

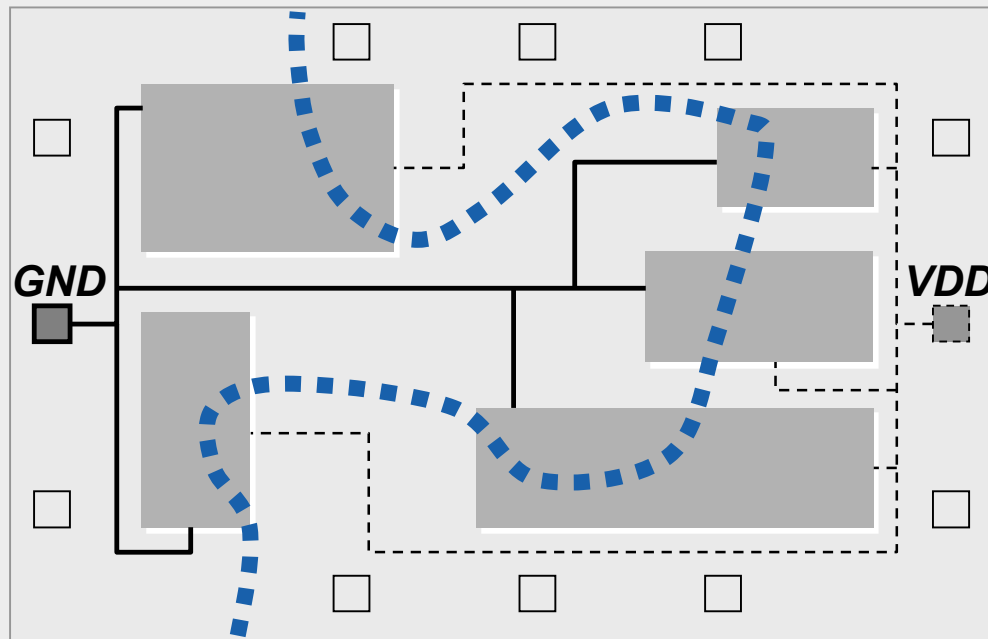
Power and ground rings  
per block or abutted blocks



Trunks connect rings to each other or to top-level power ring

## 3.7 Power and Ground Routing

Planar routing



Hamiltonian path



### Planar routing

#### Step 1: Planarize the topology of the nets

- As both power and ground nets must be routed on one layer, the design should be split using the Hamiltonian path

#### Step 2: Layer assignment

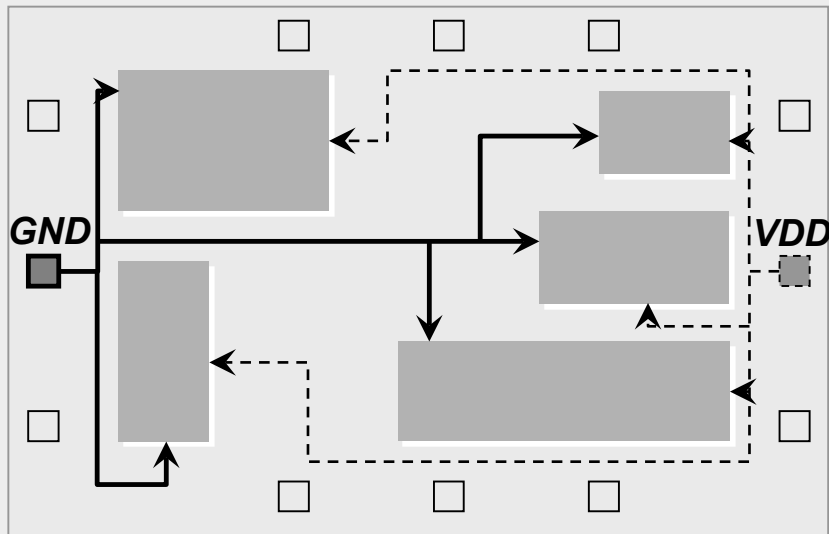
- Net segments are assigned to appropriate routing layers

#### Step 3: Determining the widths of the net segments

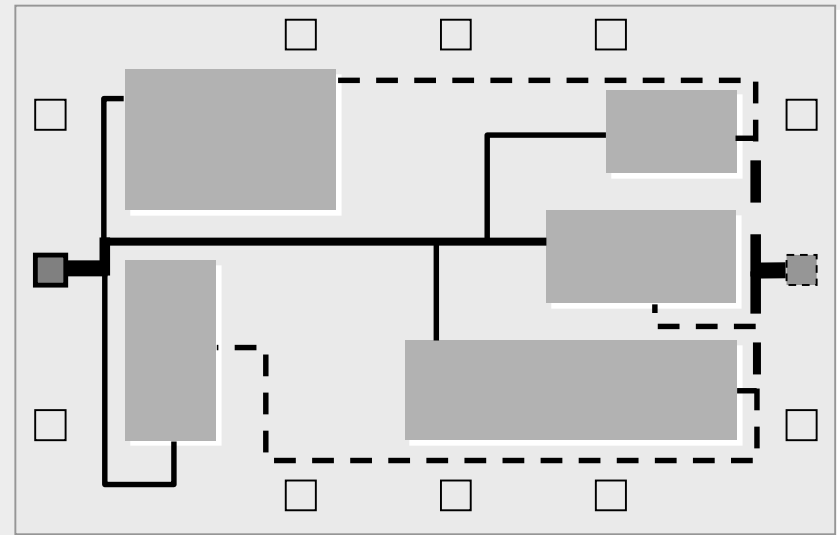
- A segment's width is determined from the sum of the currents from all the cells to which it connects

## 3.7 Power and Ground Routing

### Planar routing



Generating topology  
of the two supply nets



Adjusting widths of the segments  
with regard to their current loads

### Mesh routing

#### Step 1: Creating a ring

- A ring is constructed to surround the entire core area of the chip, and possibly individual blocks.

#### Step 2: Connecting I/O pads to the ring

#### Step 3: Creating a mesh

- A power mesh consists of a set of stripes at defined pitches on two or more layers

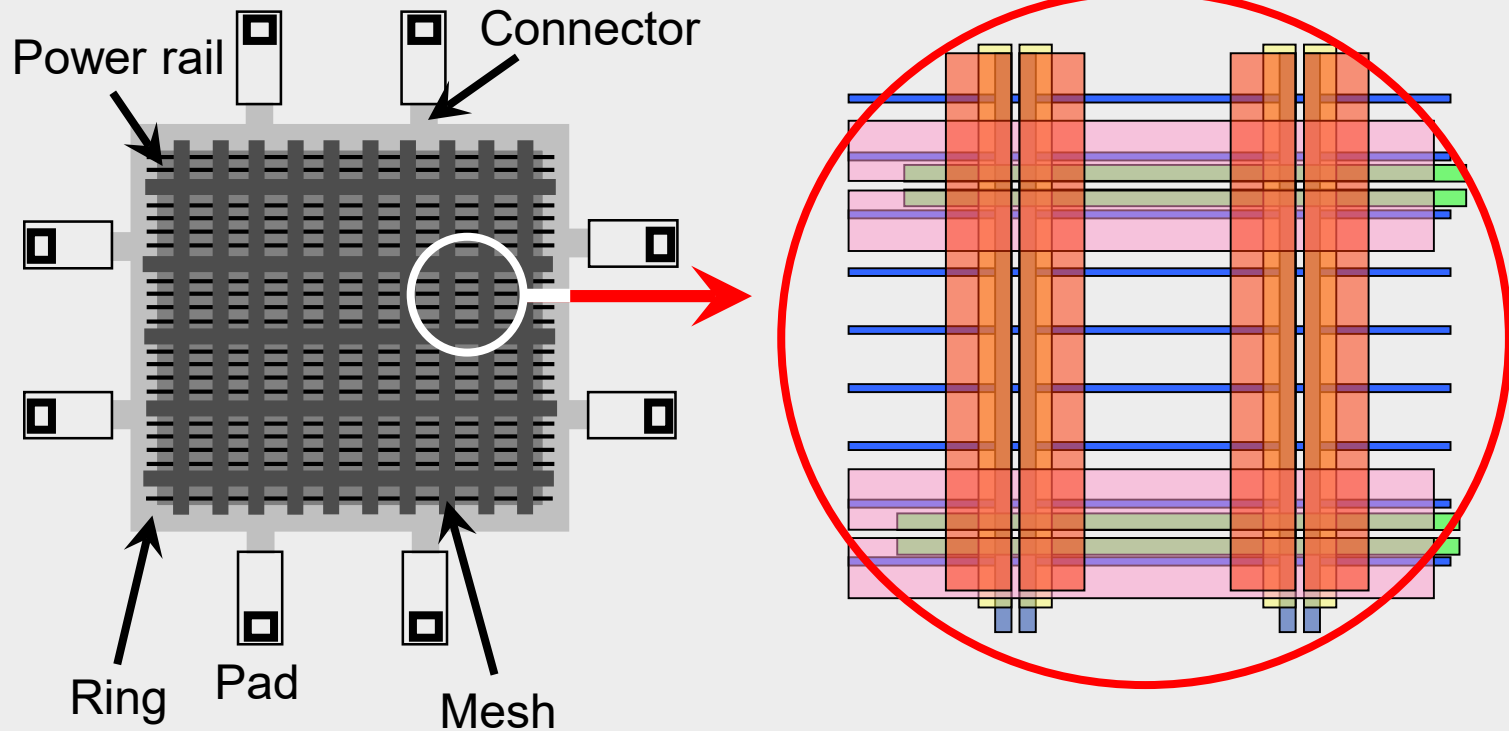
#### Step 4: Creating Metal1 rails

- Power mesh consists of a set of stripes at defined pitches on two or more layers

#### Step 5: Connecting the Metal1 rails to the mesh

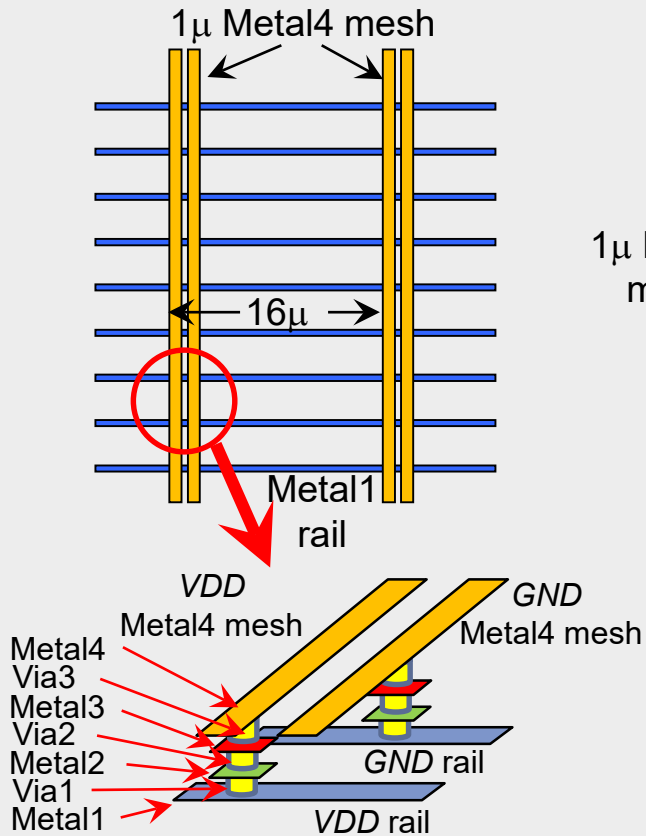
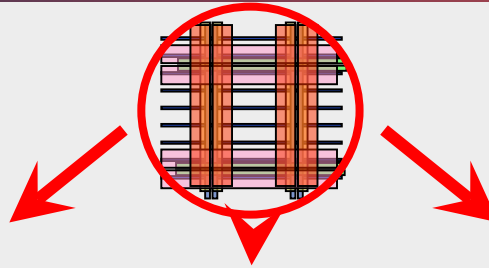
## 3.7 Power and Ground Routing

### Mesh routing

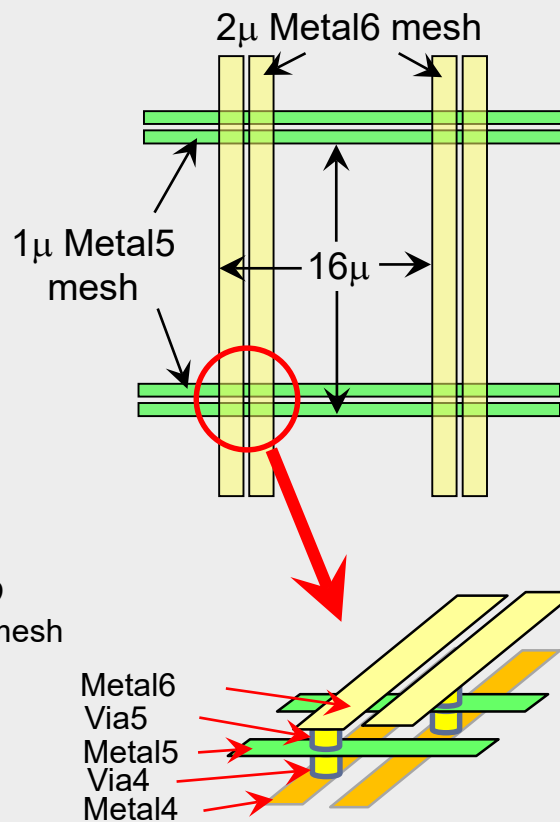


## 3.7 Power and Ground Routing

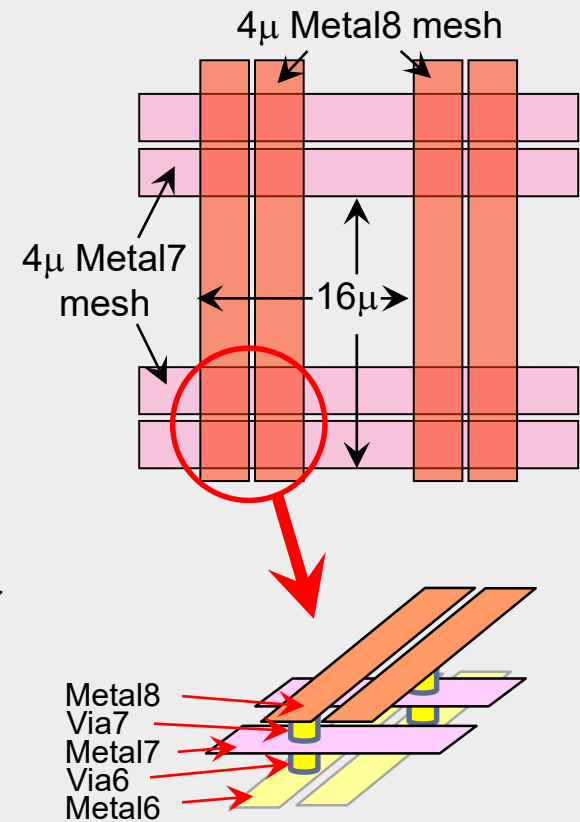
### Mesh routing



**M1-to-M4 connection**



**M4-to-M6 connection**



**M6-to-M8 connection**

# Summary of Chapter 3 – Objectives and Terminology

- Traditional floorplanning
  - Assumes area estimates for top-level circuit modules
  - Determines shapes and locations of circuit modules
  - Minimizes chip area and length of global interconnect
- Additional aspects
  - Assigning/placing I/O pads
  - Defining channels between blocks for routing and buffering
  - Design of power and ground networks
  - Estimation and optimization of chip timing and routing congestion
- Fixed-outline floorplanning
  - Chip size is fixed, focus on interconnect optimization
  - Can be applied to individual chip partitions (hierarchically)
- Structure and types of floorplans
  - Slicing versus non-slicing, the wheels
  - Hierarchical
  - Packed
  - Zero-deadspace

## Summary of Chapter 3 – Data Structures for Floorplanning

- Slicing trees and Polish expressions
  - Evaluating a floorplan represented by a Polish expression
- Horizontal and vertical constraint graphs
  - A data structure to capture (non-slicing) floorplans
  - Longest paths determine floorplan dimensions
- Sequence pair
  - An array-based data structure that captures the information contained in H+V constraint graphs
  - Makes constraint graphs unnecessary in practice
- Floorplan sizing
  - Shape-function arithmetic
  - An algorithm for slicing floorplans

# Summary of Chapter 3 – Algorithms for Floorplanning

- Cluster growth
  - Simple, fast and intuitive
  - Not competitive in practice
- Simulated annealing
  - Stochastic optimization with hill-climbing
  - Many details required for high-quality implementation (e.g., temperature schedule)
  - Difficult to debug, fairly slow
  - Competitive in practice
- Pin assignment
  - Peripheral I/Os versus area-array I/Os
  - Given "ideal locations", project them onto perimeter and shift around, while preserving initial ordering
- Power and ground routing
  - Planar routing in channels between blocks
  - Can form rings around blocks to increase current supplied and to improve reliability
  - Mesh routing